

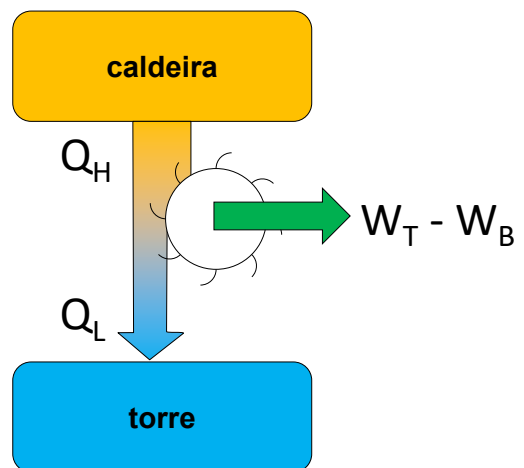
CURSO INTENSIVO

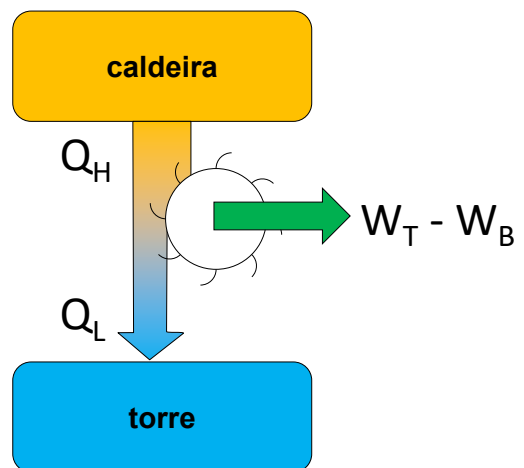
# TERMODINÂMICA E APLICAÇÕES DE ENGENHARIA

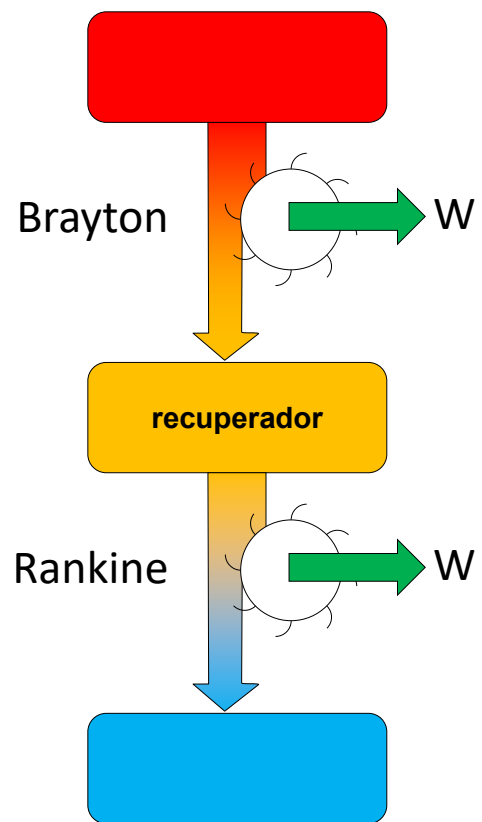
## CICLOS DE POTÊNCIA A VAPOR – Parte 1 o ciclo motor de Rankine

Paulo Seleghim Jr.  
Universidade de São Paulo

Attention to  
Filler Words

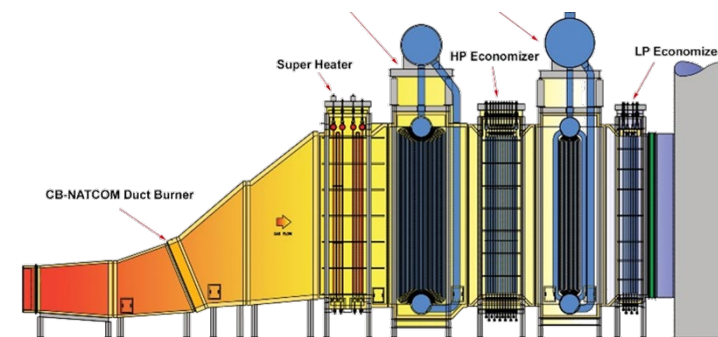




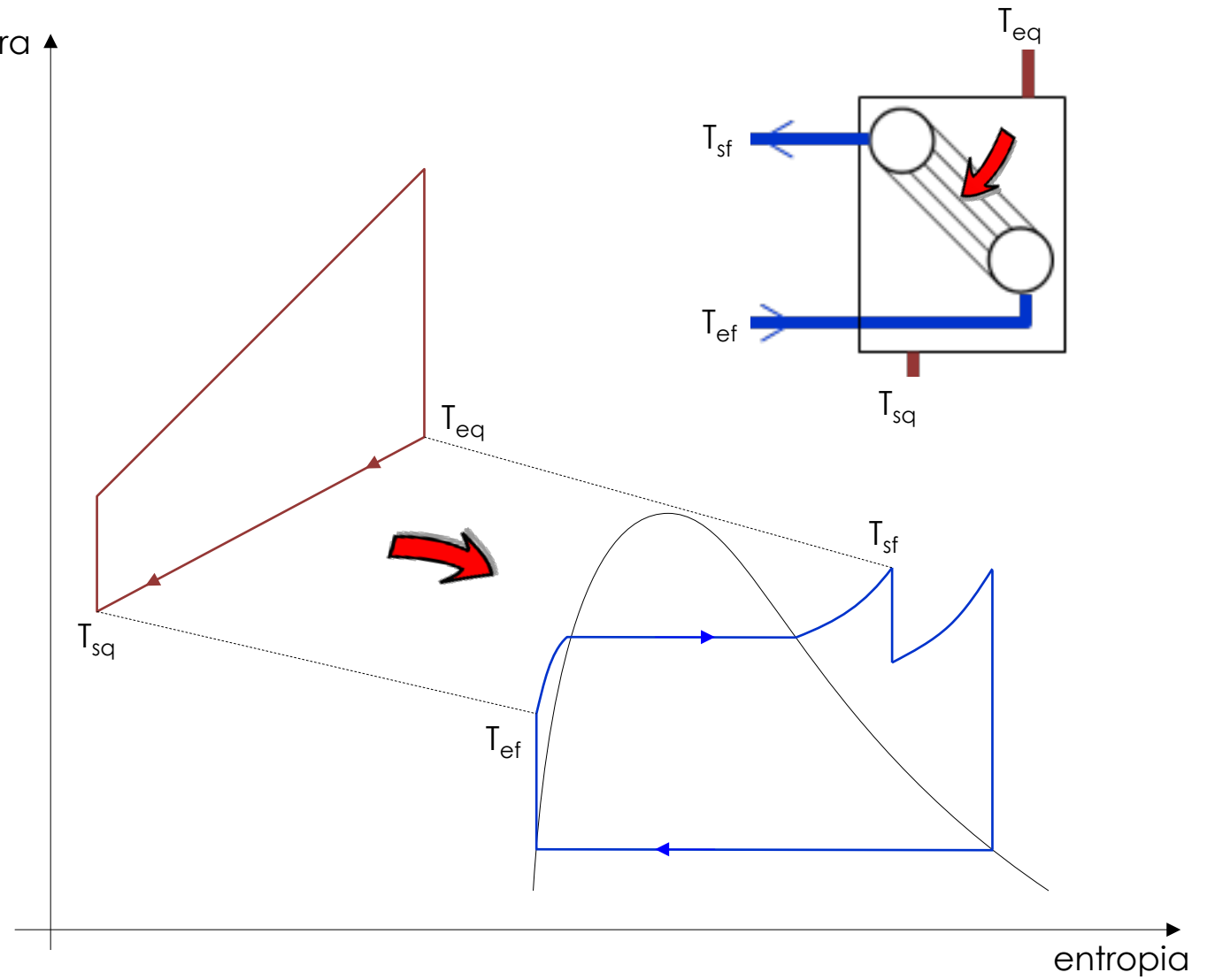
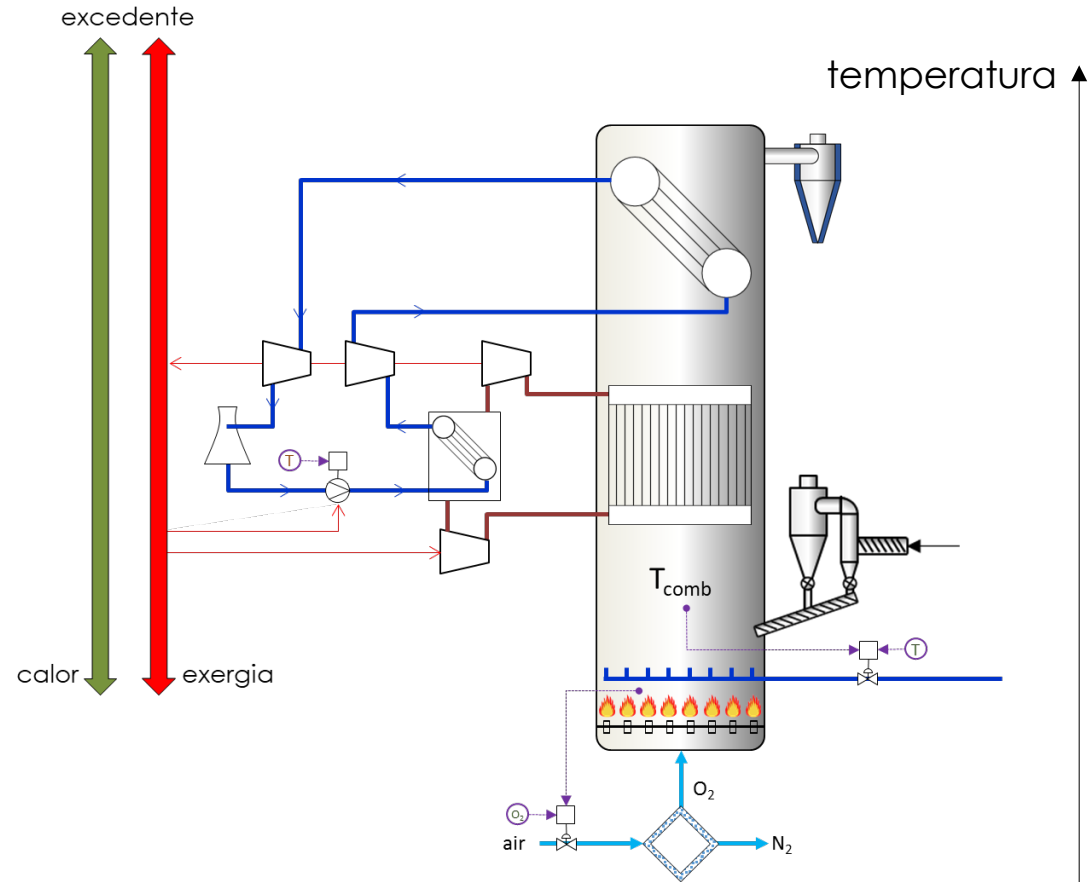


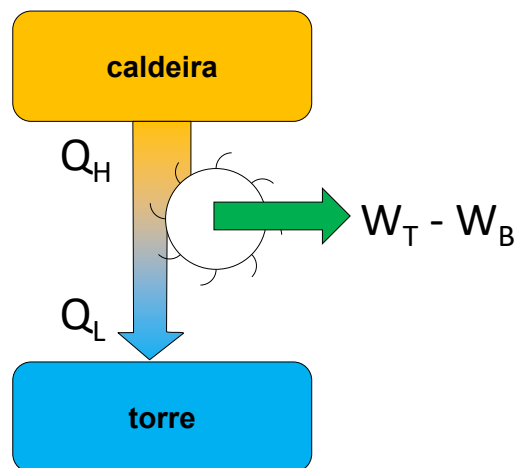
Aulas 14 e 15: Ciclos Avançados

## Ciclos combinados / avançados

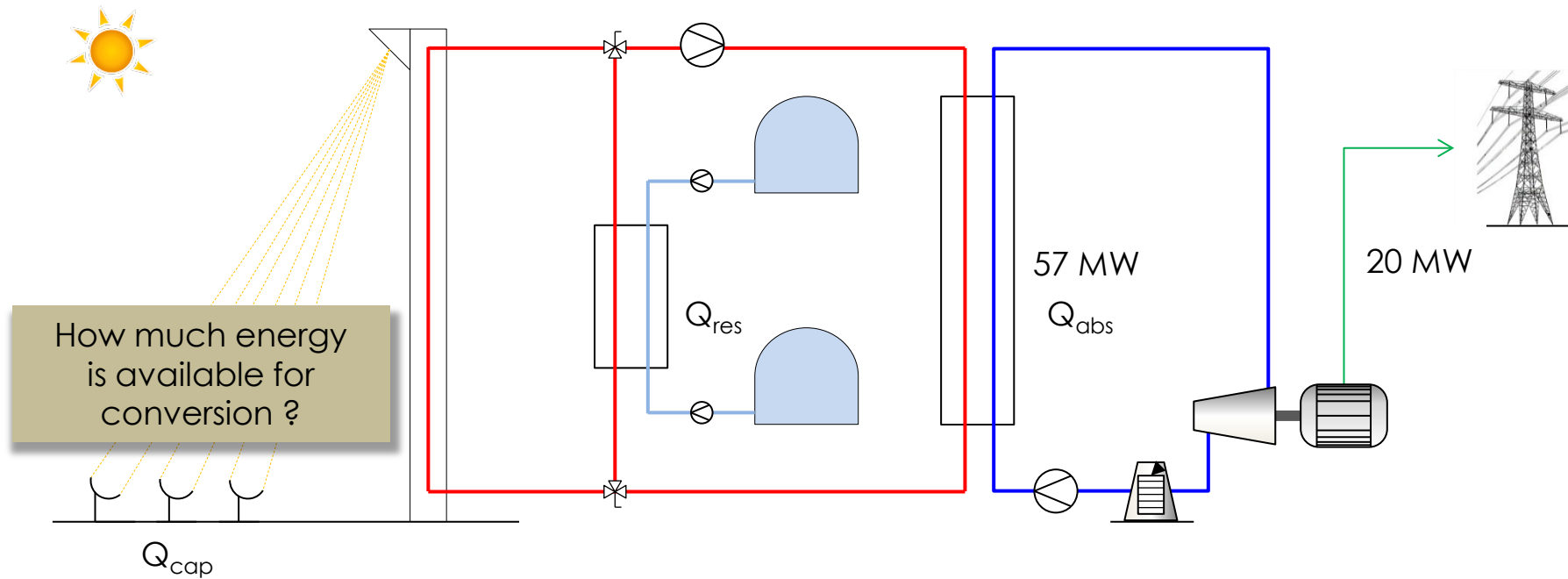


# Ciclo de Brayton associado a um ciclo de Rankine com reaquecimento





# CONCEPTUAL DESIGN OF A THERMOSOLAR POWER PLANT...



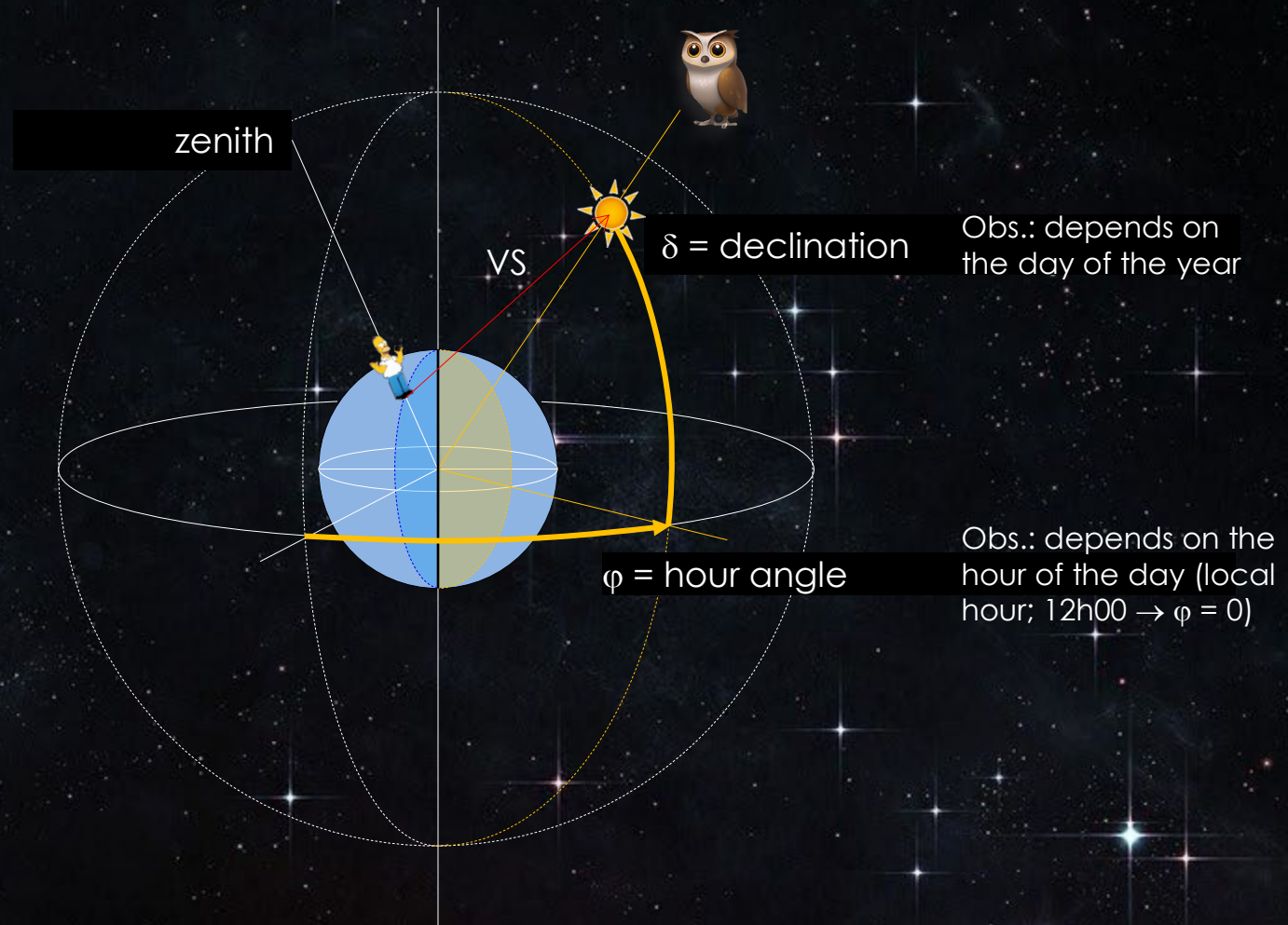
Average solar energy ( $W/m^2$ ) collected at earth's surface by a 2D collector placed at latitude  $\phi$ , disregarding the presence of clouds and other random losses.

$$\bar{Q}_{cap}(\phi) \cong \frac{1}{365 \cdot 12} \int_{\text{day}} \int_{\text{hour}} (\text{solar energy}) d\phi dn$$



# Definitions and working formulae...

## SUN'S EQUATORIAL COORDINATES



# Definitions and working formulae...

Definition of the day of the year and of the hour of the day

$$n = 1, 2 \dots 365 \quad \varphi = -90^\circ, -89^\circ, \dots + 90^\circ$$

Calculus of the solar elevation (h):

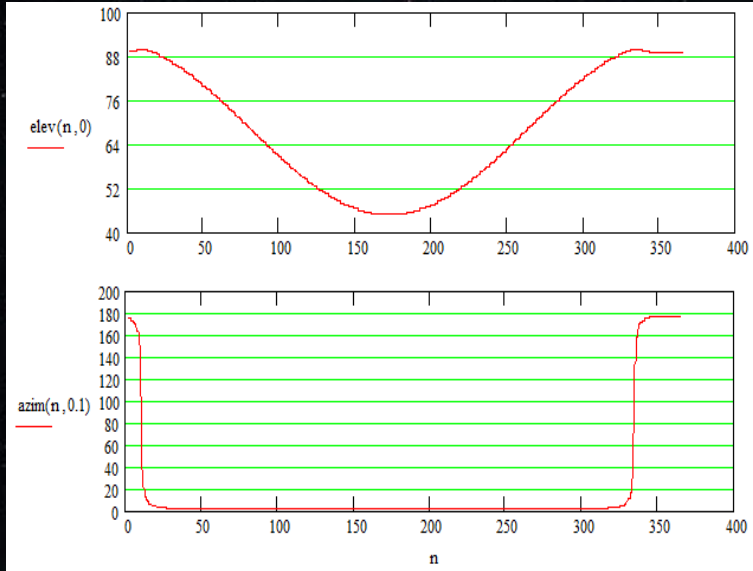
$$\sin(h) = \sin(\phi)\sin(\delta) + \cos(\phi)\cos(\delta)\cos(\varphi)$$

Calculus of the solar azimuth (A):

$$\cos(A) = \frac{\sin(\phi)\sin(h) - \sin(\delta)}{\cos(\phi)\cos(h)}$$

Definition of the solar vector (VS):

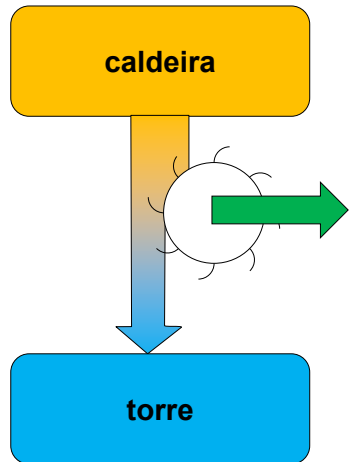
$$VS = \cos(h) \cos(A) \hat{i} + \cos(h) \sin(A) \hat{j} + \sin(h) \hat{k}$$



Sun's elevation at noon in São Carlos (22°01''S = -22,017°)

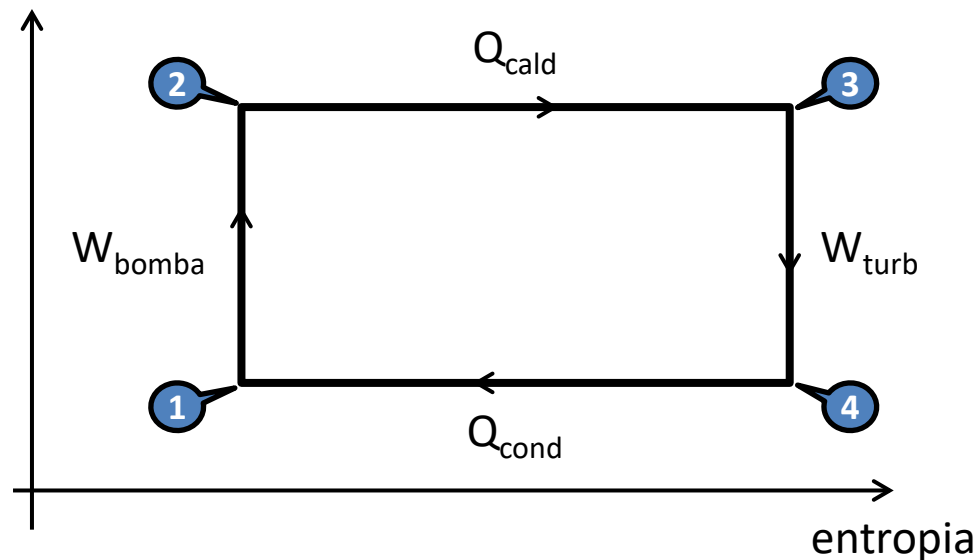
# Análise dos ciclos a vapor: O ciclo de Rankine

# Ciclo de Carnot: definição



- 1-2) Compressão isentrópica (bomba)
- 2-3) Aquecimento isotérmico (caldeira)
- 3-4) Expansão isentrópica (turbina)
- 4-1) Resfriamento isotérmico (condensador)

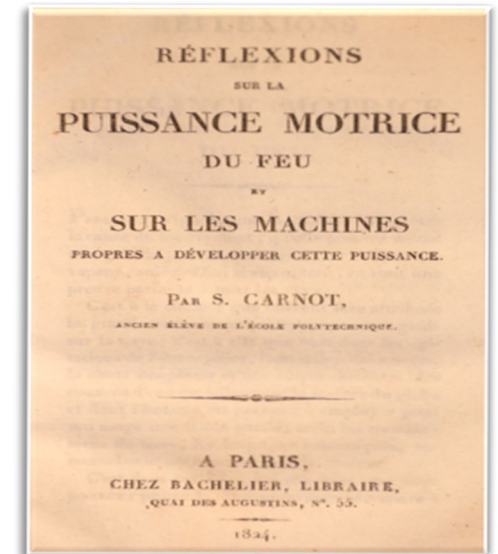
temperatura



Attention to  
Filler Words

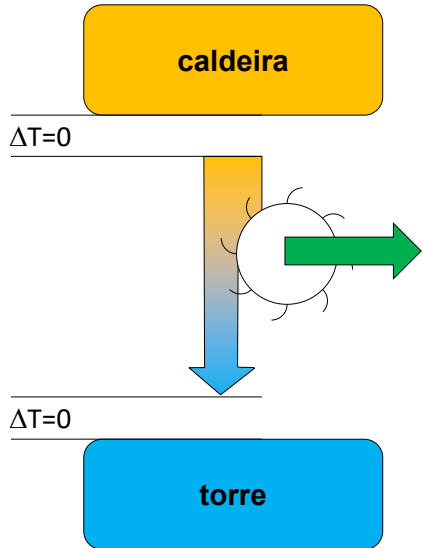


Nicolas Léonard Sadi Carnot  
em 1824, aos 28 anos de idade...

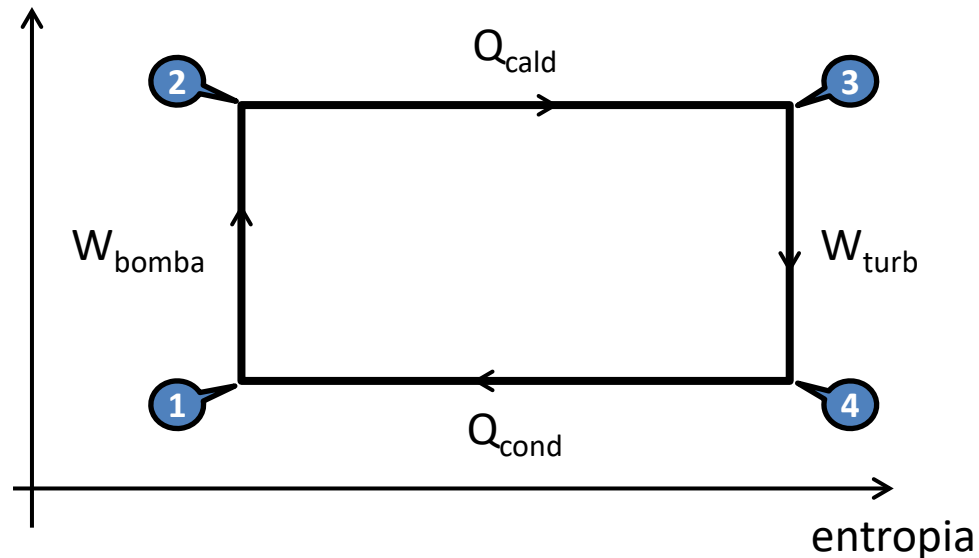


# Ciclo de Carnot: definição

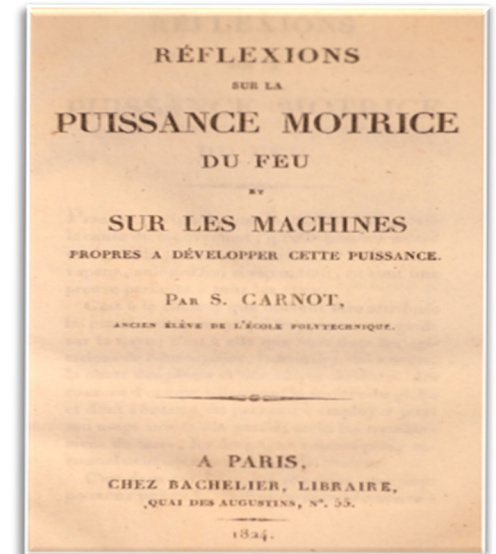
- 1-2) Compressão isentrópica (bomba)
- 2-3) Aquecimento isotérmico (caldeira)
- 3-4) Expansão isentrópica (turbina)
- 4-1) Resfriamento isotérmico (condensador)



temperatura

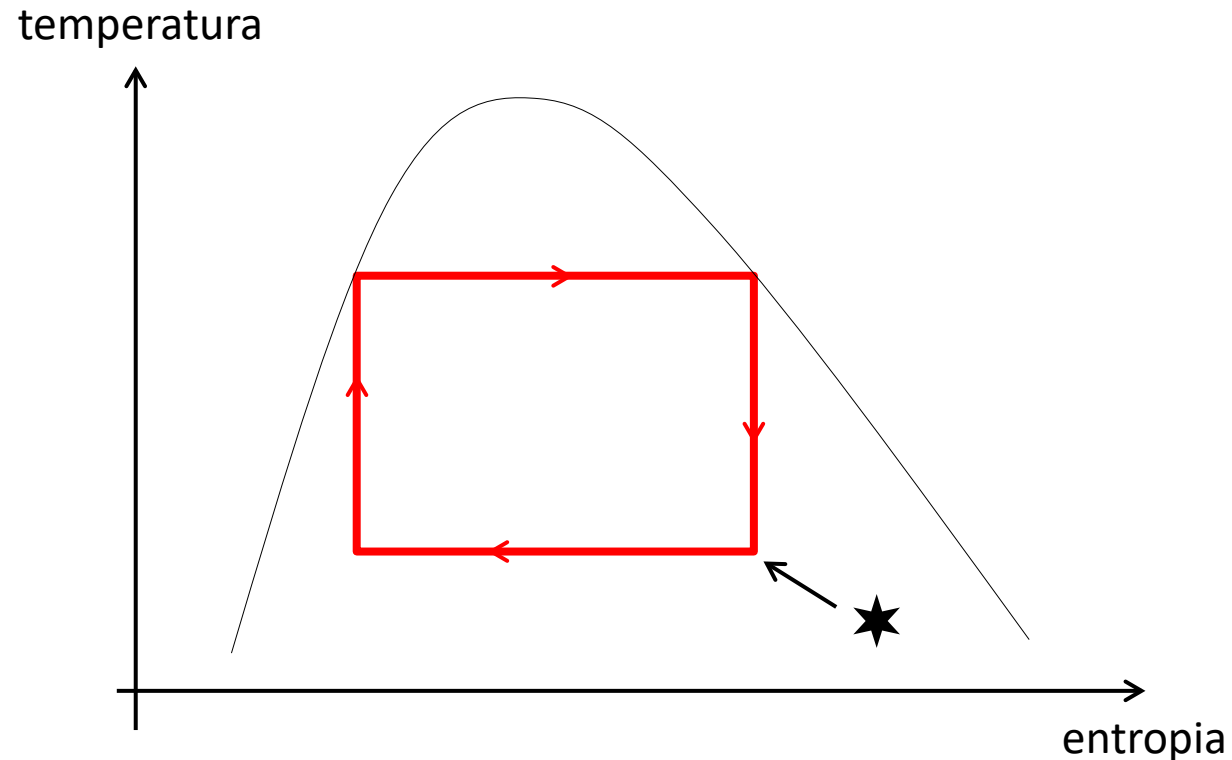


Nicolas Léonard Sadi Carnot em 1824, aos 28 anos de idade...



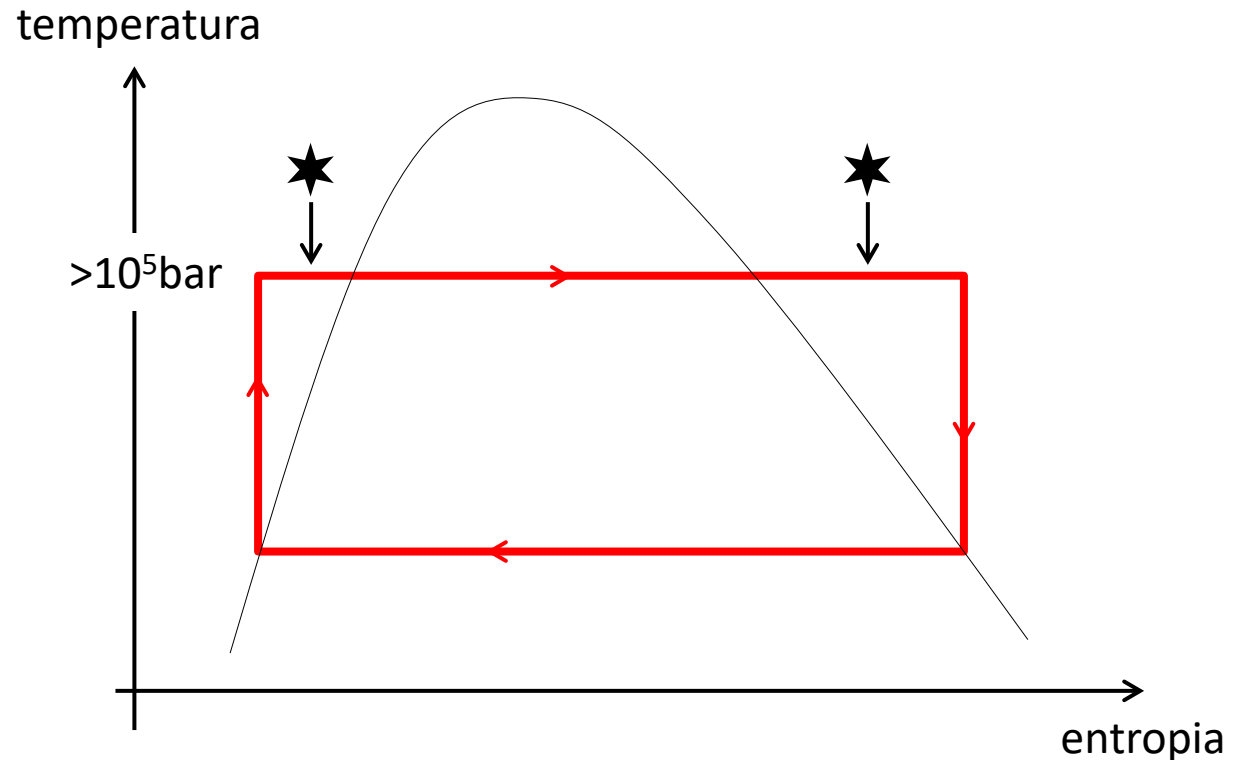
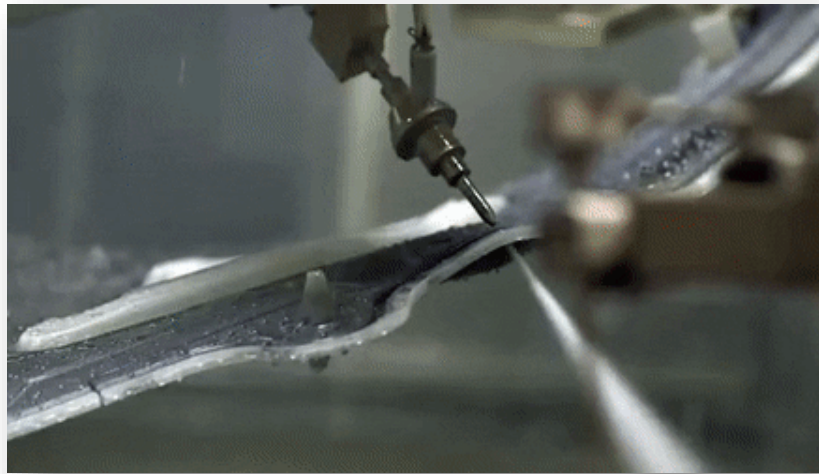
# Ciclo de Carnot: dificuldades de realização prática

- Okay controle da temperatura
- Erosão na turbina devido à formação de gotas (★)
- Baixa eficiência hidromecânica no bombeamento de uma mistura bifásica



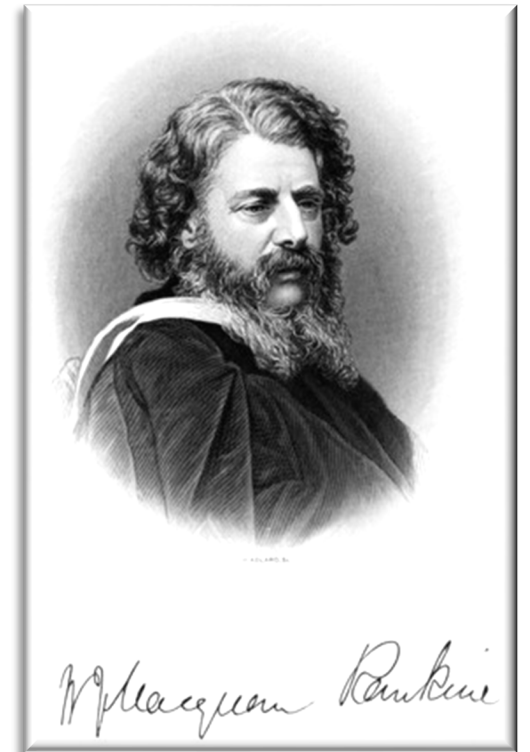
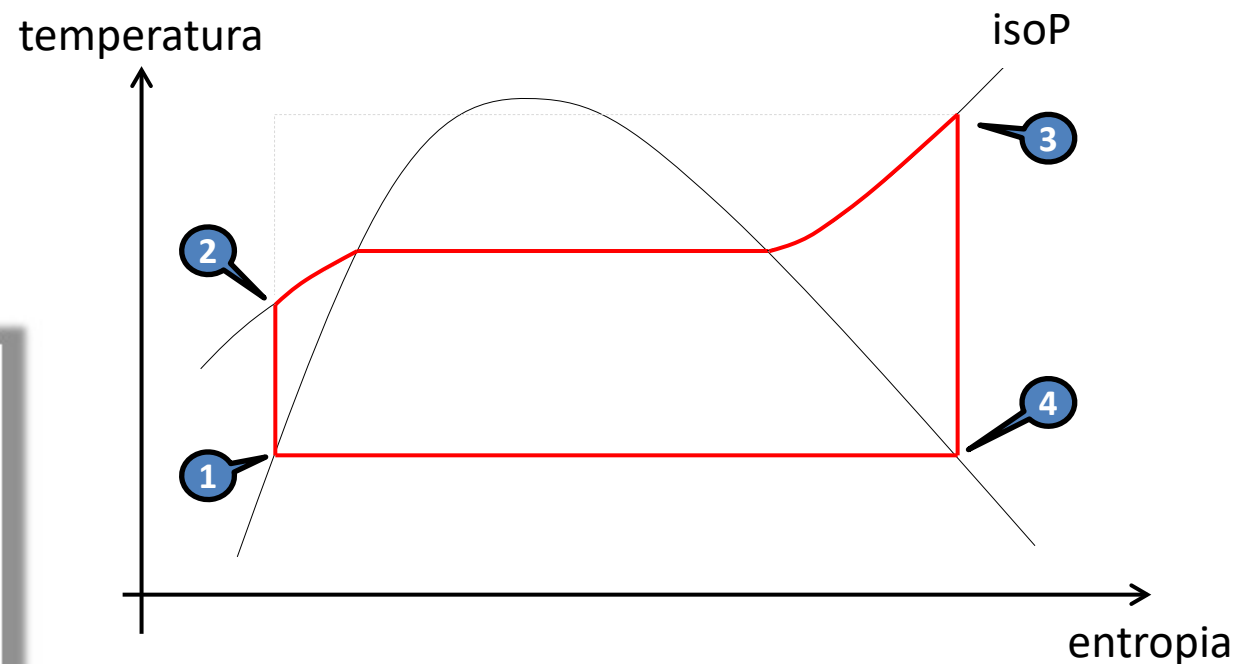
# Ciclo de Carnot: dificuldades de realização prática

- Okay bomba, turbina e controle da temperatura condensador
- Pressão líquido comprimido impossivelmente elevada
- Difícil controle da temperatura nas regiões monofásicas (★)



# Ciclo de Rankine: definição

- 1-2) Compressão isentrópica (bomba)
- 2-3) Aquecimento isobárico (caldeira)
- 3-4) Expansão isentrópica (turbina)
- 4-1) Resfriamento isotérmico (condensador)



William John Macquorn Rankine

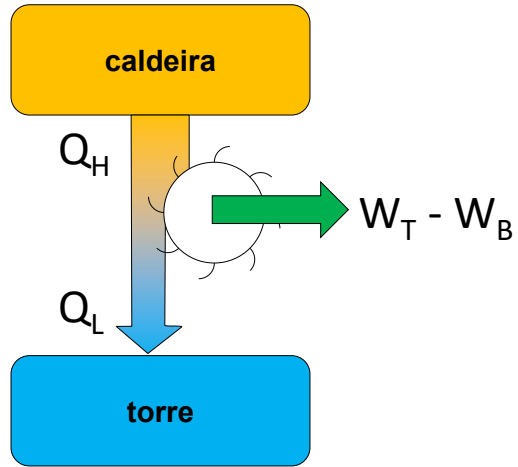




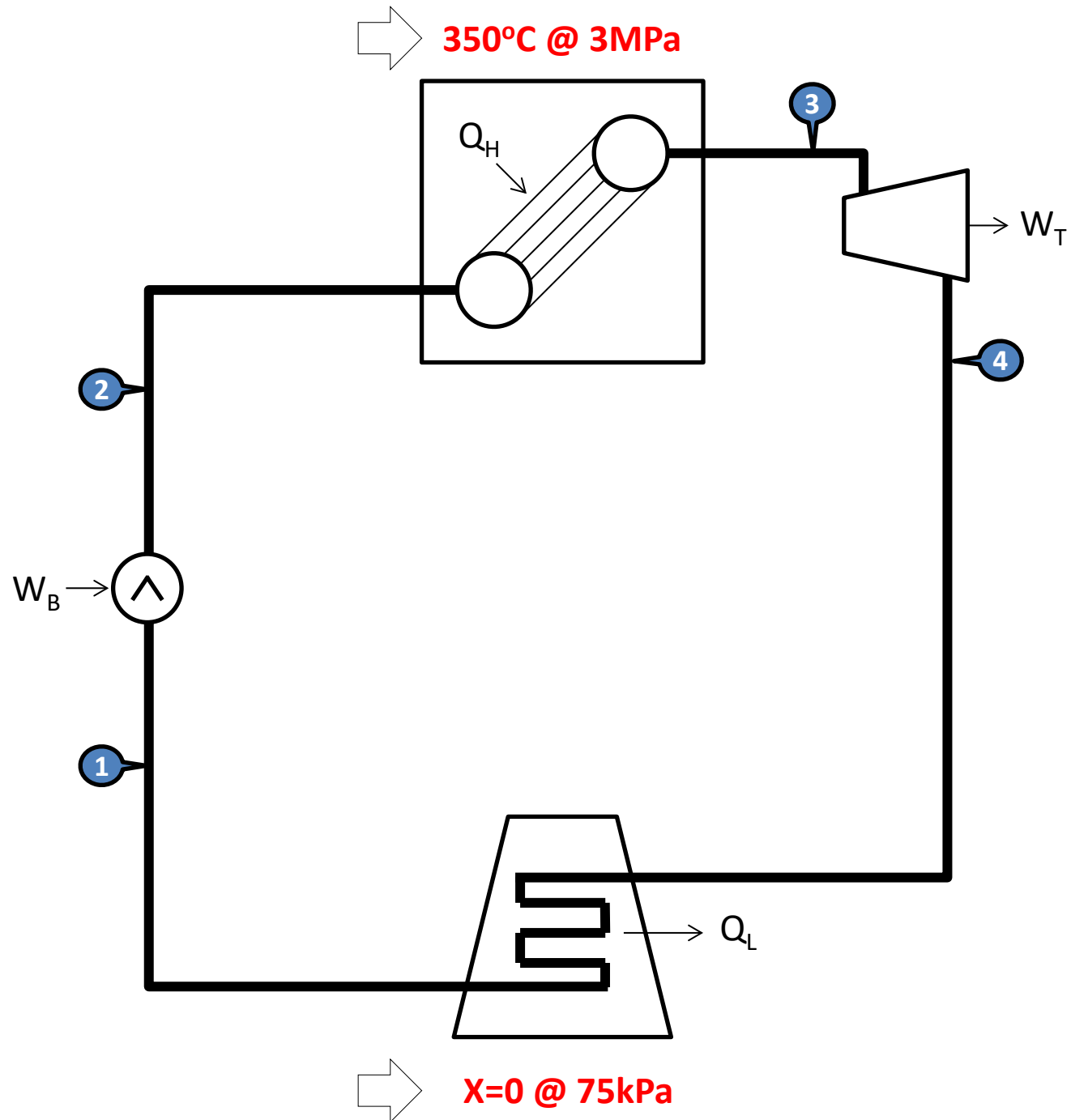
**Exemplos...**

## Ciclo de Rankine Padrão

- 1-2: bombeamento isentrópico
- 2-3: aquecimento isobárico
- 3-4: expansão isentrópica
- 4-1: resfriamento isobárico



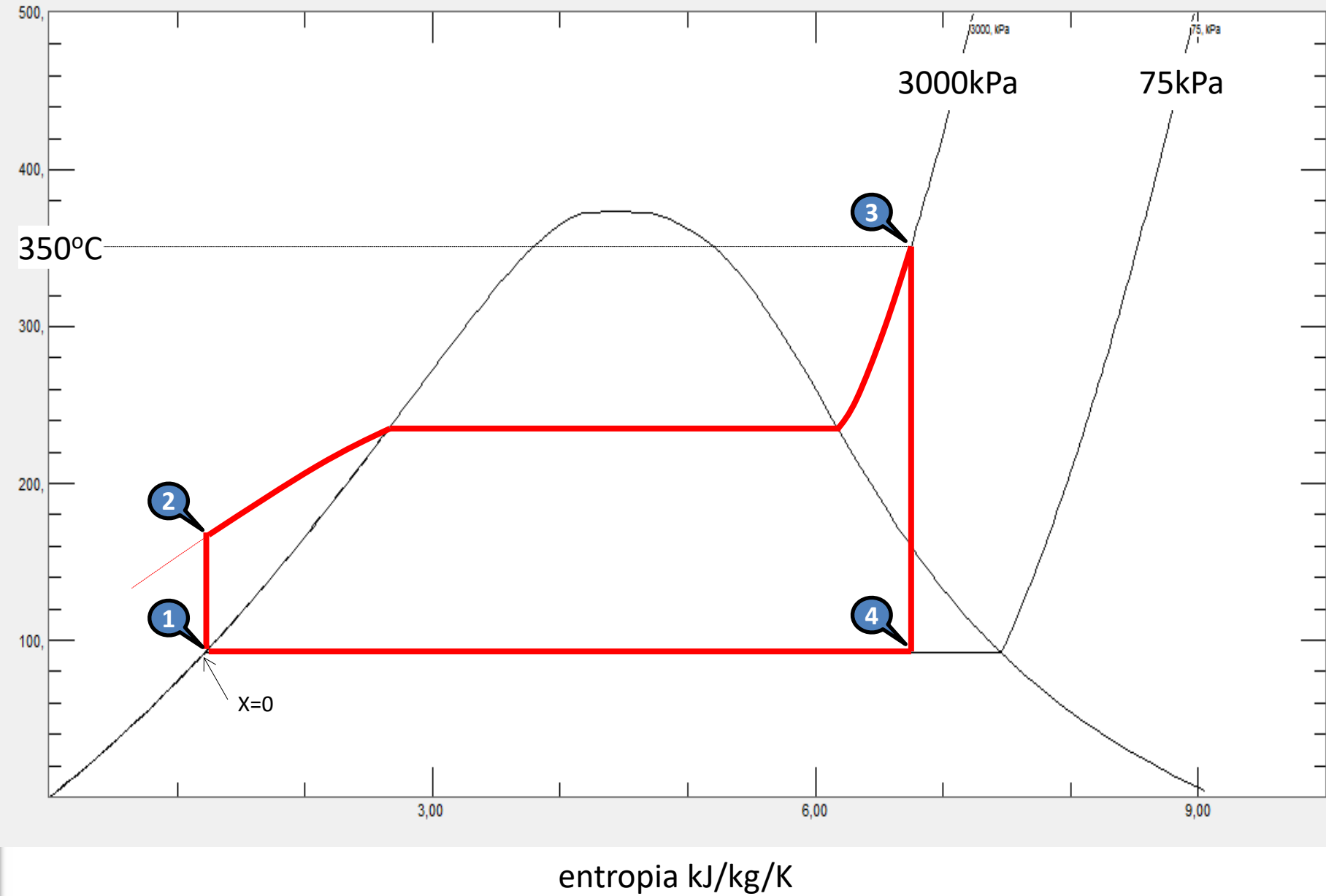
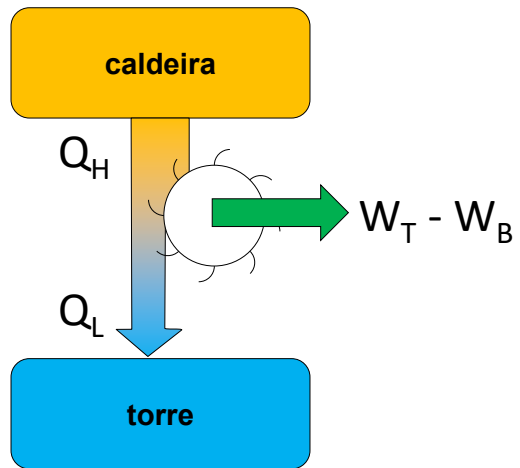
Attention to  
Filler Words



temperatura °C

### Ciclo de Rankine Padrão

- 1-2: bombeamento isentrópico
- 2-3: aquecimento isobárico
- 3-4: expansão isentrópica
- 4-1: resfriamento isobárico

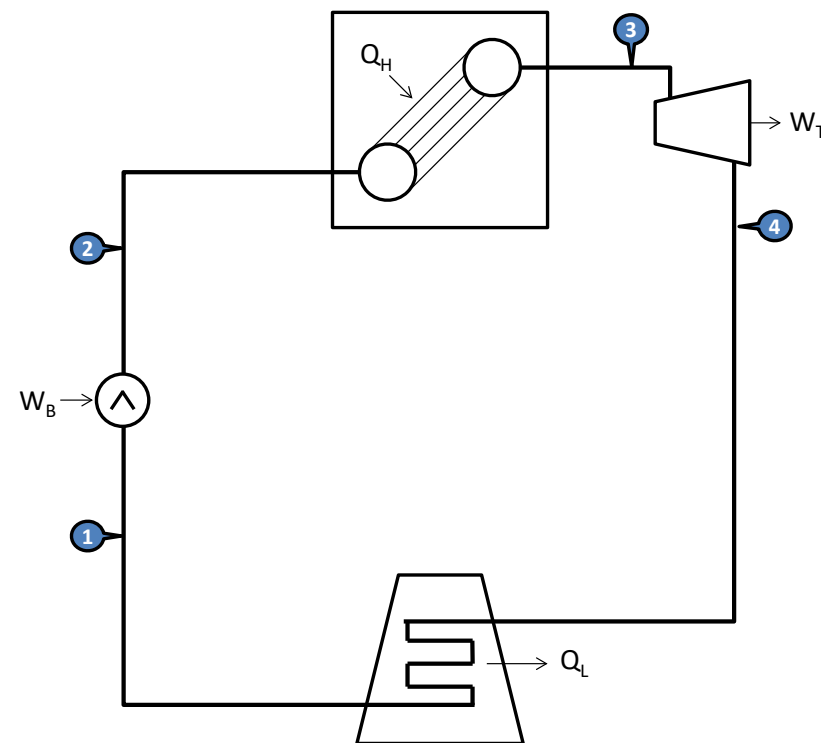


# Cálculo do trabalho demandado pela bomba

$$Q_{bba} - W_{bba} = \dot{m} \cdot h_2 - \dot{m} \cdot h_1$$

$$\cancel{Q_{bba}} - W_{bba} = \dot{m} \cdot h_2 - \dot{m} \cdot h_1$$

$$\frac{W_{Bba}}{\dot{m}} = h_1 - h_2$$



⇒  $w_{bba} = h_1 - h_2$

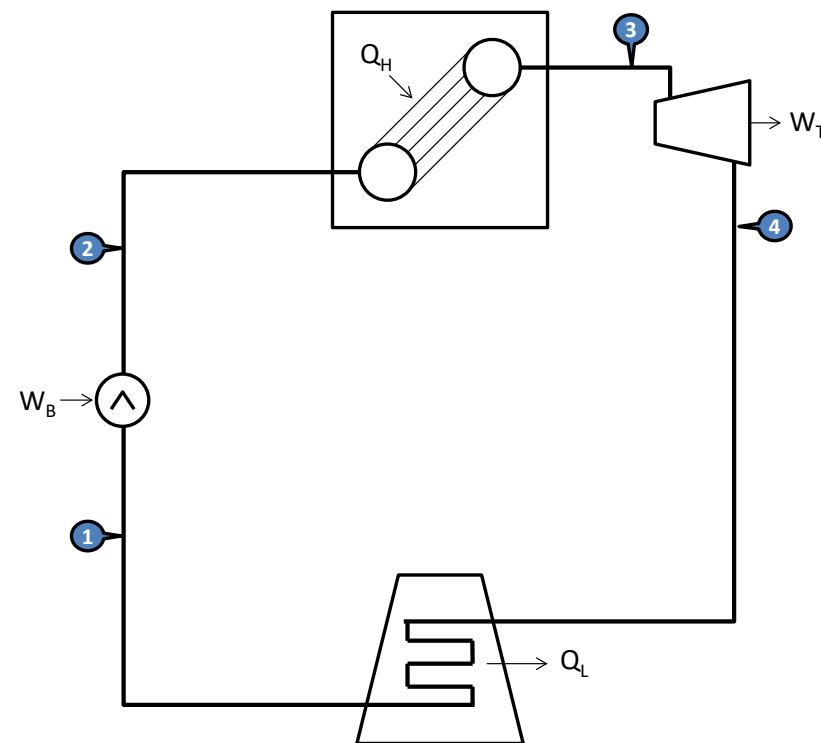
⇒  $w_{bba} < 0 \rightarrow$  absorvido

# Cálculo do calor gerado na caldeira

$$Q_{\text{cal}} - W_{\text{cal}} = \dot{m} \cdot h_3 - \dot{m} \cdot h_2$$

$$Q_{\text{cal}} - \cancel{W_{\text{cal}}} = \dot{m} \cdot h_3 - \dot{m} \cdot h_2$$

$$\frac{Q_{\text{cal}}}{\dot{m}} = h_3 - h_2$$



⇒  $q_{\text{cal}} = h_3 - h_2$

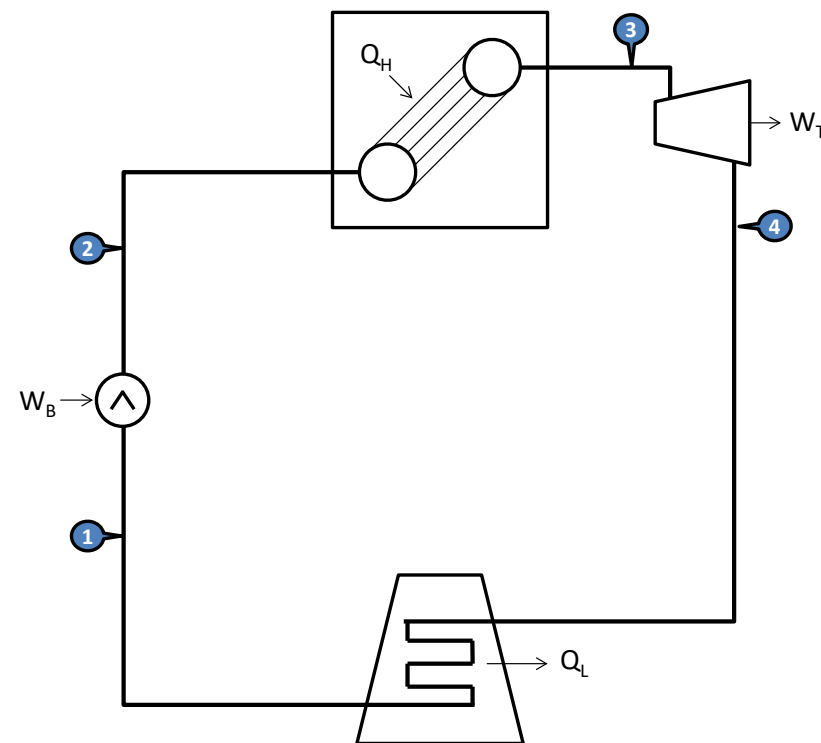
⇒  $q_{\text{cal}} > 0 \rightarrow \text{absorvido}$

# Cálculo do trabalho produzido na turbina

$$Q_{\text{tur}} - W_{\text{tur}} = \dot{m} \cdot h_4 - \dot{m} \cdot h_3$$

~~$$Q_{\text{tur}} - W_{\text{tur}} = \dot{m} \cdot h_4 - \dot{m} \cdot h_3$$~~

$$\frac{W_{\text{tur}}}{\dot{m}} = h_3 - h_4$$



⇒  $w_{\text{tur}} = h_3 - h_4$

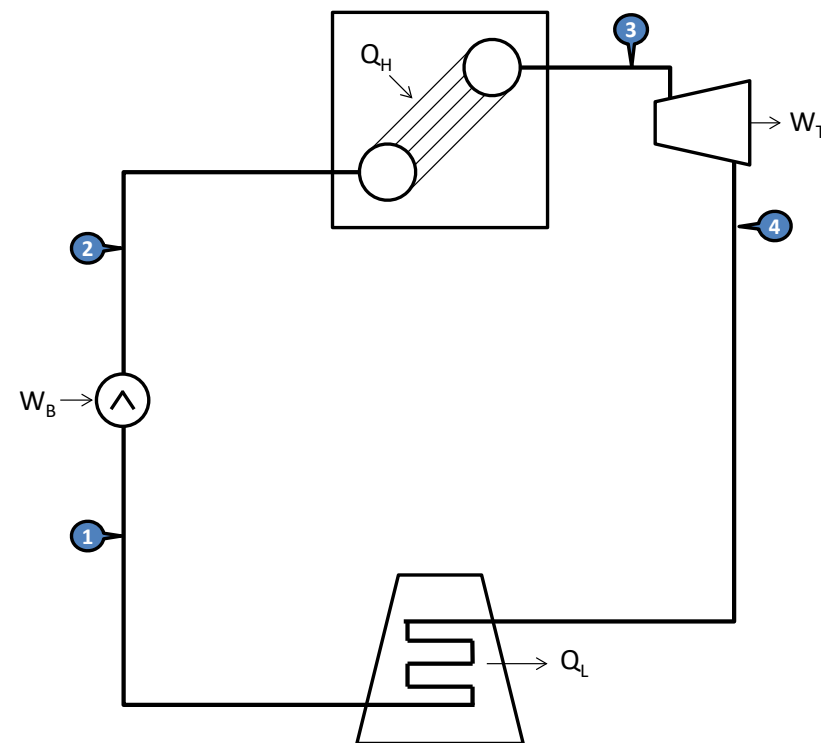
⇒  $w_{\text{tur}} > 0 \rightarrow \text{rejeitado}$

# Cálculo do calor rejeitado na torre de resfriamento

$$Q_{\text{con}} - W_{\text{con}} = \dot{m} \cdot h_1 - \dot{m} \cdot h_4$$

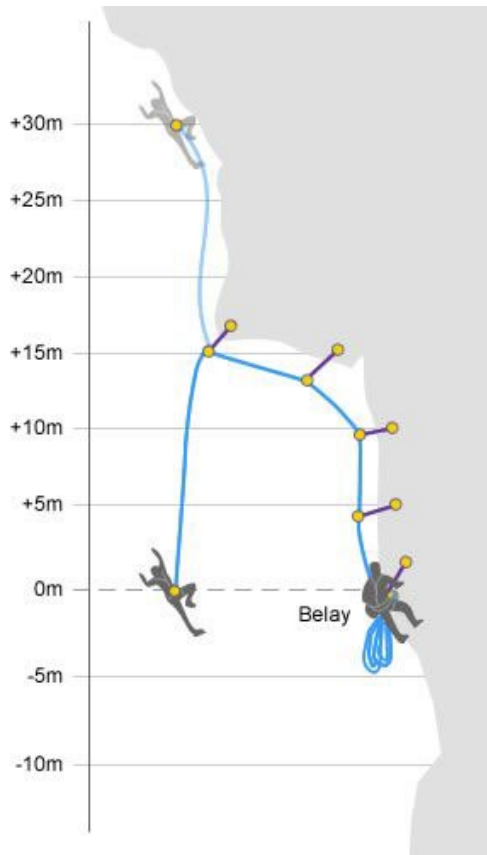
$$Q_{\text{con}} - \cancel{W_{\text{con}}} = \dot{m} \cdot h_1 - \dot{m} \cdot h_4$$

$$\frac{Q_{\text{con}}}{\dot{m}} = h_1 - h_4$$



➡  $q_{\text{con}} = h_1 - h_4$

➡  $q_{\text{con}} < 0 \rightarrow \text{rejeitado}$



$$x = 0 @ 75\text{kPa}$$



$$h_1 = 384,44 \text{ kJ/kg/K}$$

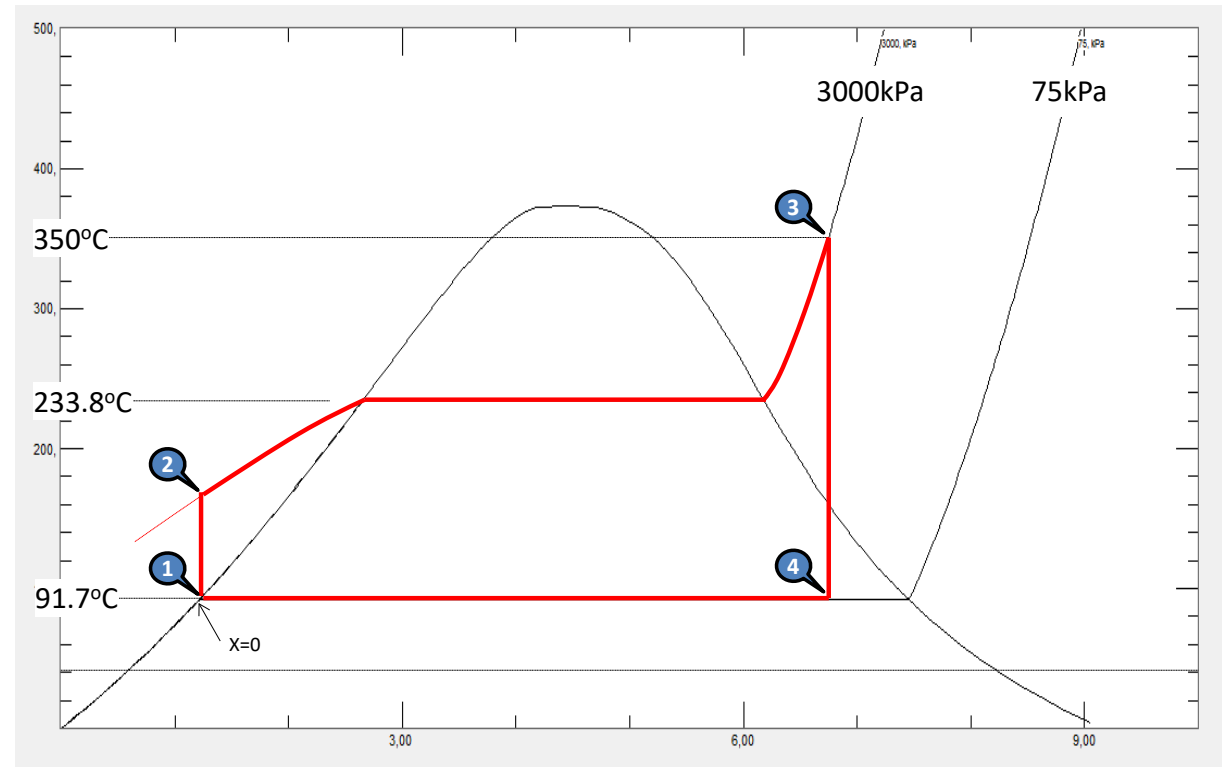
$$s_1 = 1,2132 \text{ kJ/kg/K}$$

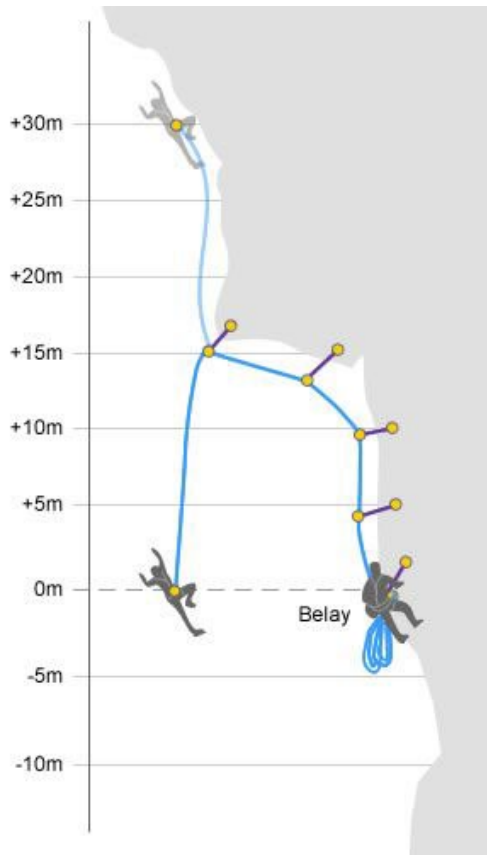
$$S_1 = S_2 @ 3\text{MPa}$$



$$h_2 = 387,44 \text{ kJ/kg/K}$$

$$T_2 = 91,946 \text{ }^\circ\text{C}$$





350°C @ 3MPa



$$h_3 = 3116,1 \text{ kJ/kg}$$

$$s_3 = 6,7449 \text{ kJ/kg/K}$$

$S_3 = S_4 @ 75\text{kPa}$



$$s_{\text{liq}} = 1,2132 \text{ kJ/kg/K}$$

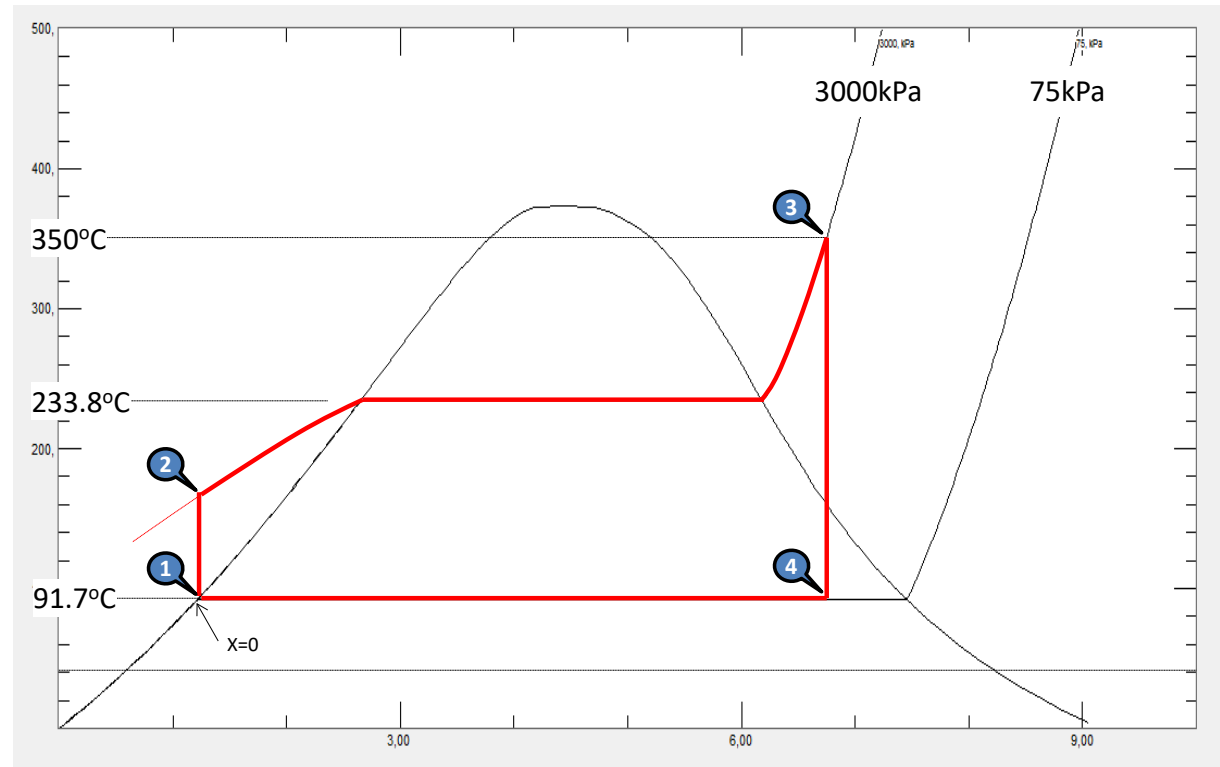
$$s_{\text{vap}} = 7,4557 \text{ kJ/kg/K}$$

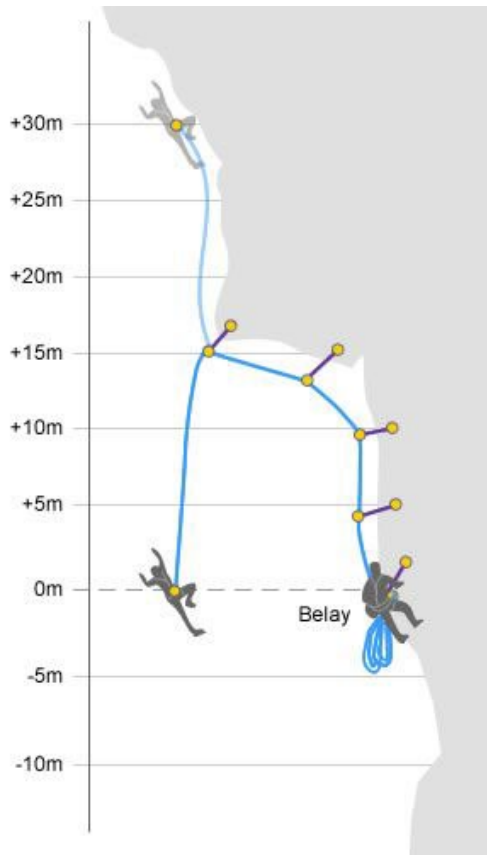
$$x = 0,886$$

$$h_{\text{liq}} = 384,45 \text{ kJ/kg}$$

$$h_{\text{vap}} = 2662,4$$

$$h_4 = 2402,7 \text{ kJ/kg}$$



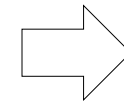


$$\eta = \frac{\sum W_T - \sum W_B}{\sum Q_C}$$

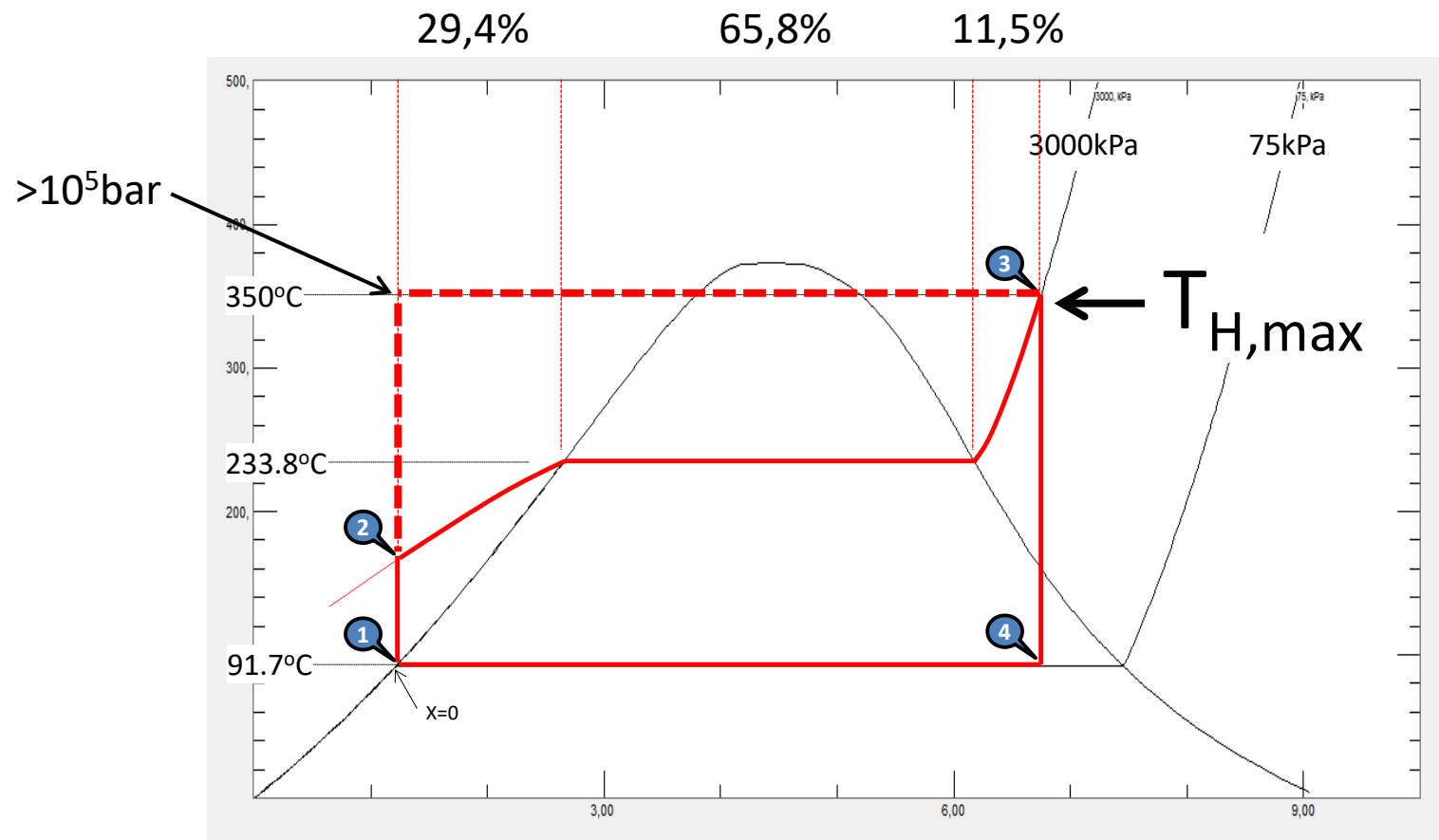
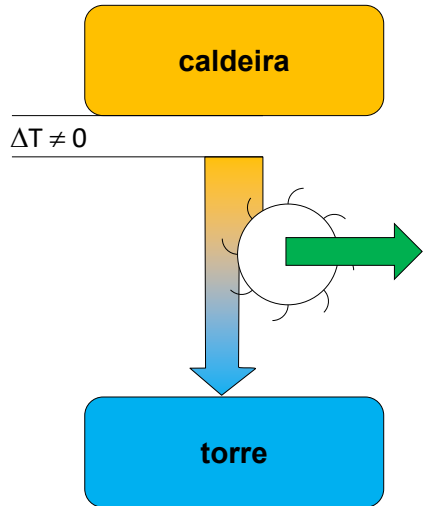
$$\eta = \frac{(h_3 - h_4) - (h_2 - h_1)}{(h_3 - h_2)}$$

$$\eta = \frac{(3116,1 - 2402,7) - (387,48 - 384,44)}{(3116,1 - 387,48)}$$

$$\eta = 0,263$$



$$\eta = 0,263$$



$$\left. \begin{array}{l} T_{L,min} = 91,7^\circ\text{C} \\ T_{H,max} = 350^\circ\text{C} \end{array} \right\}$$

$$\eta_{\text{Carnot}} = 1 - T_L/T_H$$

$$\eta_{\text{Carnot}} = 1 - (91.7+273)/(350+273)$$

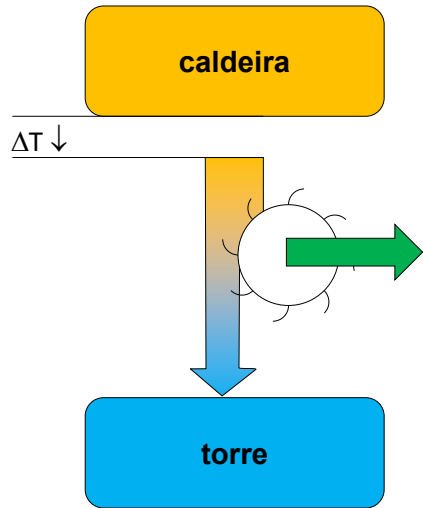
$$\eta_{\text{Carnot}} = 0,415 \quad \eta_{\text{Rankine}} = 0,263$$

Absorção de calor a baixas temperaturas



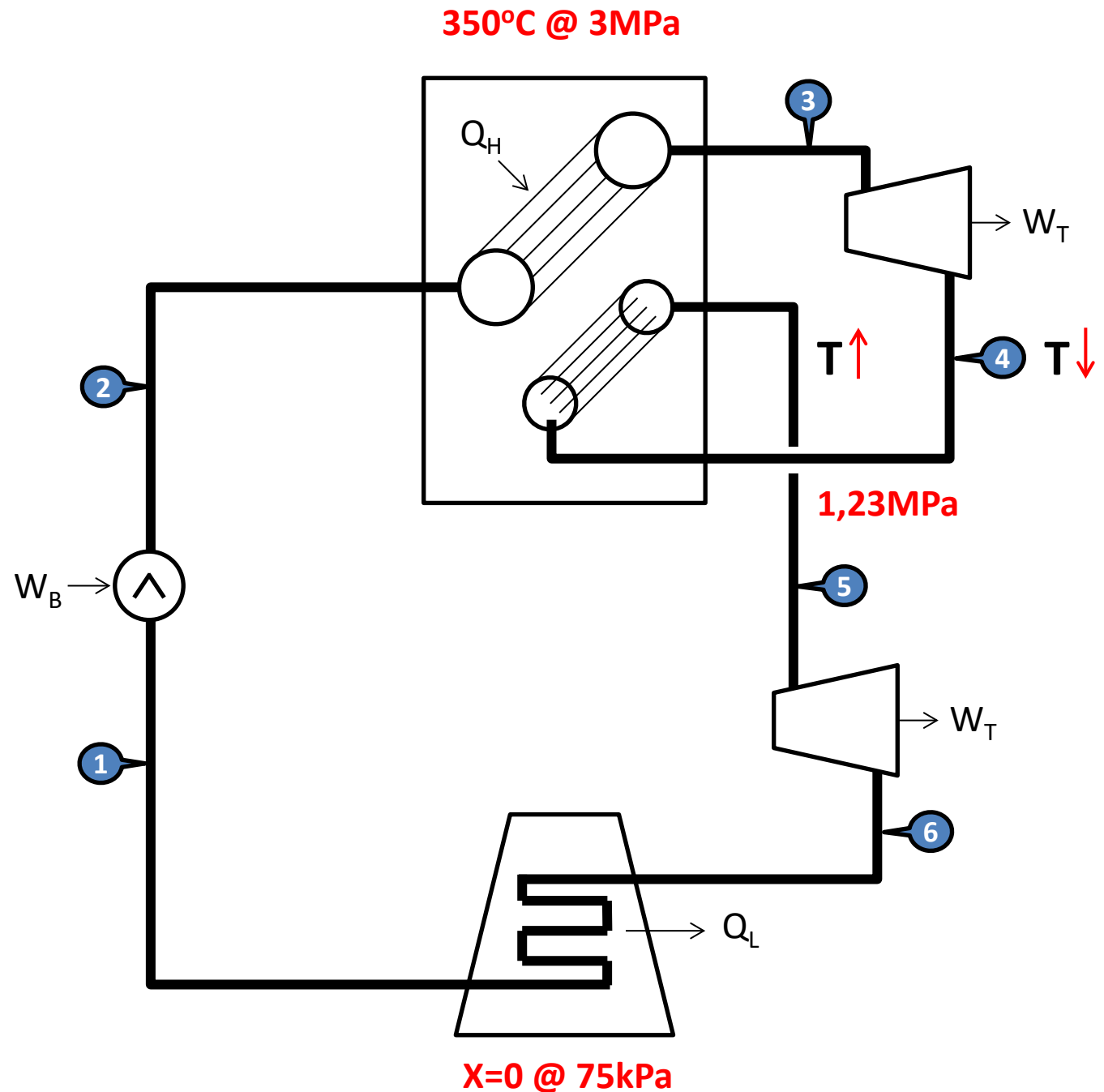
Redução da eficiência de conversão

# Ciclo de Rankine com reaquecimento de vapor

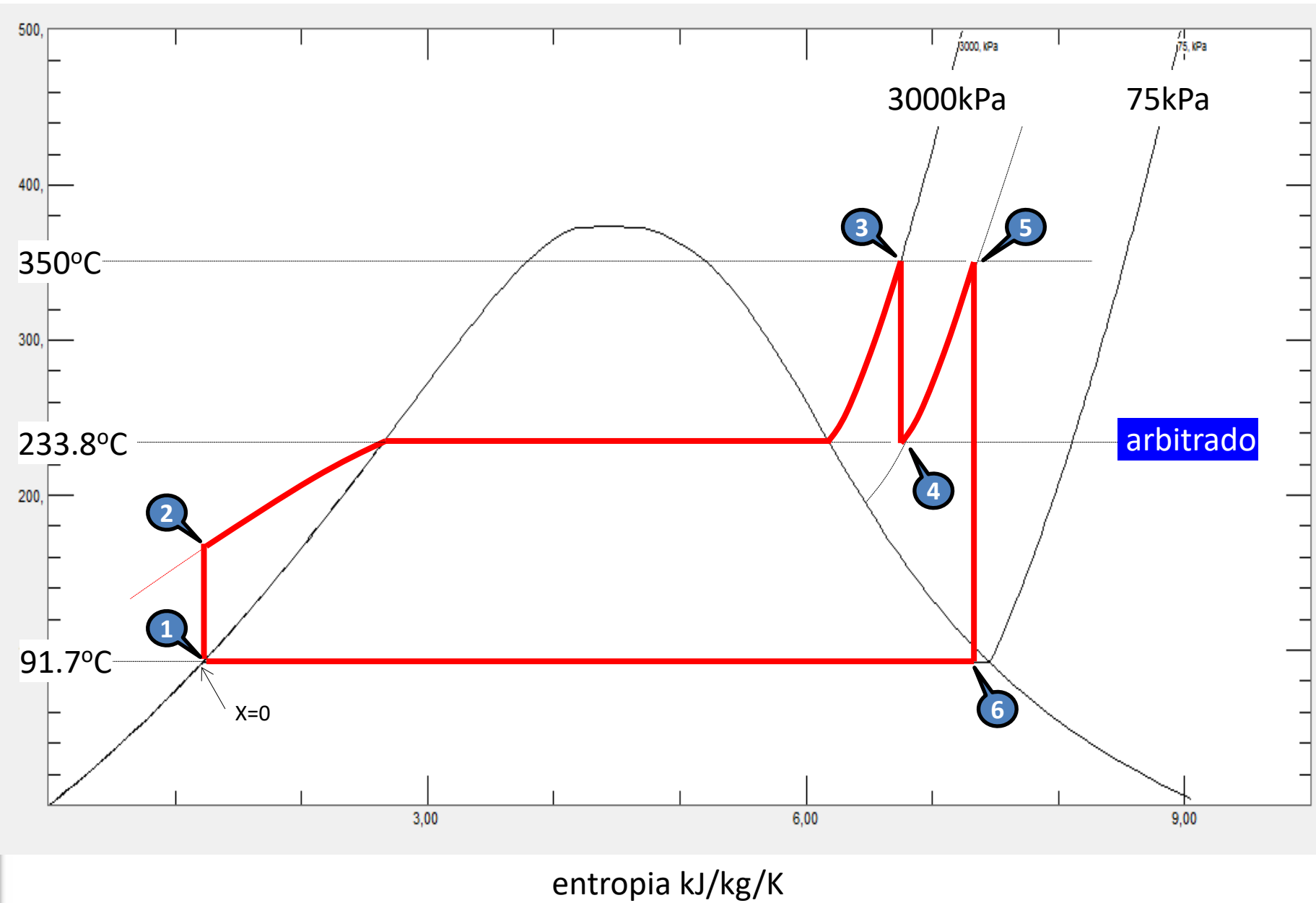
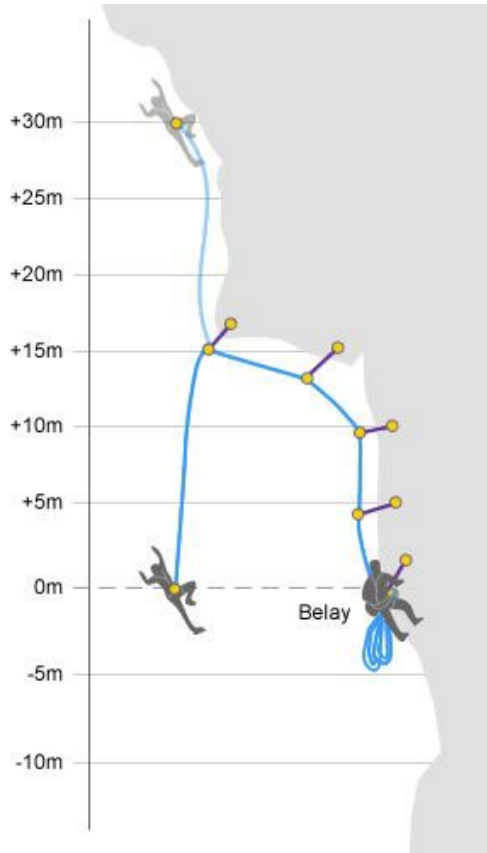


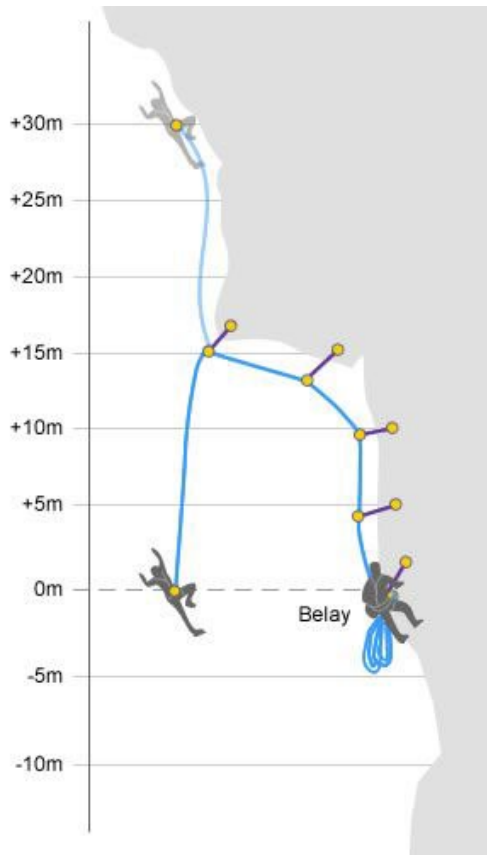
$$\eta = \frac{w_{12} + w_{34} + w_{56}}{q_{23} + q_{45}}$$

Attention to  
Filler Words



temperatura °C





$$x = 0 @ 75\text{kPa}$$



$$h_1 = 384,44 \text{ kJ/kg/K}$$

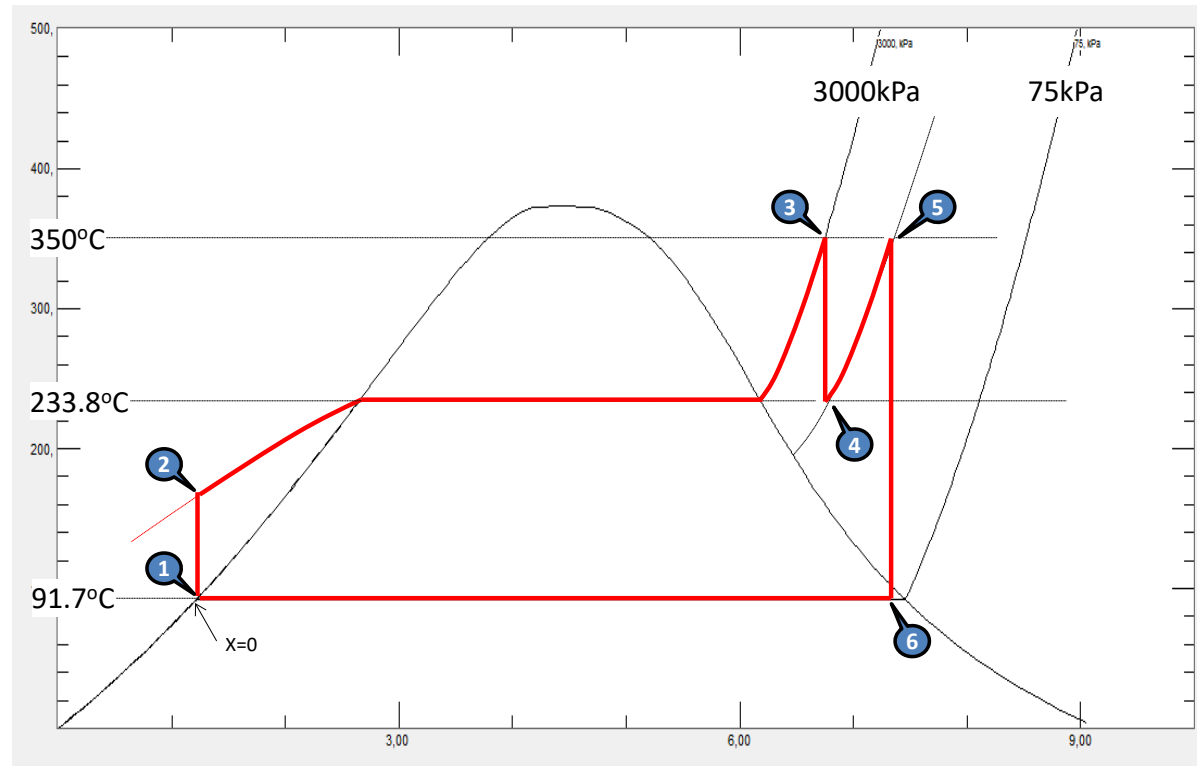
$$s_1 = 1,2132 \text{ kJ/kg/K}$$

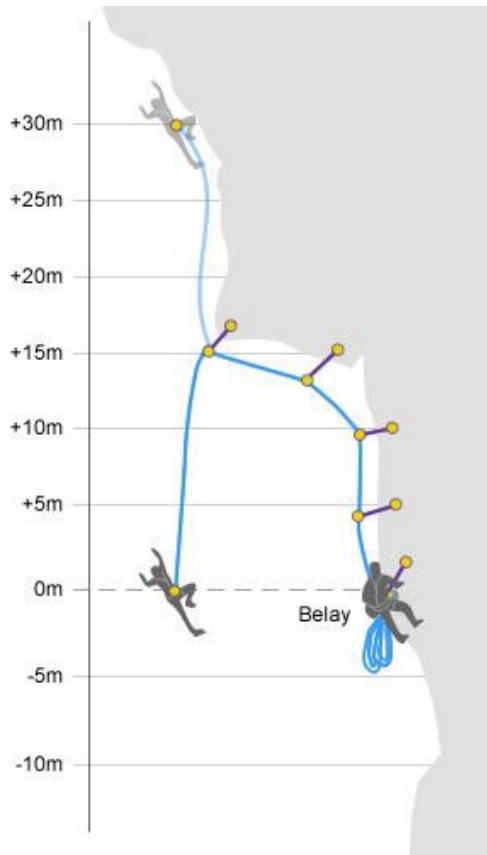
$$S_1 = S_2 @ 3\text{MPa}$$



$$h_2 = 387,48 \text{ kJ/kg/K}$$

$$T_2 = 91,946 \text{ }^\circ\text{C}$$





350°C @ 3MPa



$$h_3 = 3116,1 \text{ kJ/kg}$$

$$s_3 = 6,7449 \text{ kJ/kg/K}$$

$S_3 = S_4 @ T_{\text{sat}} / 3\text{MPa}$

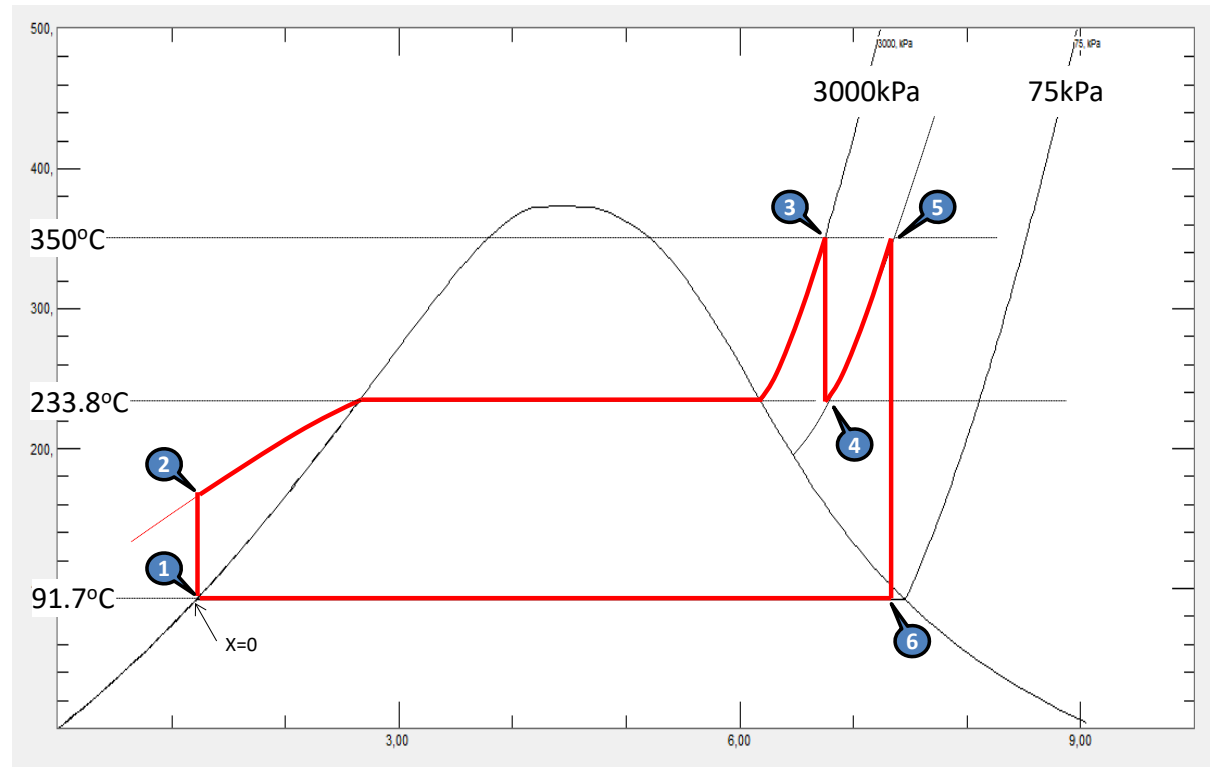


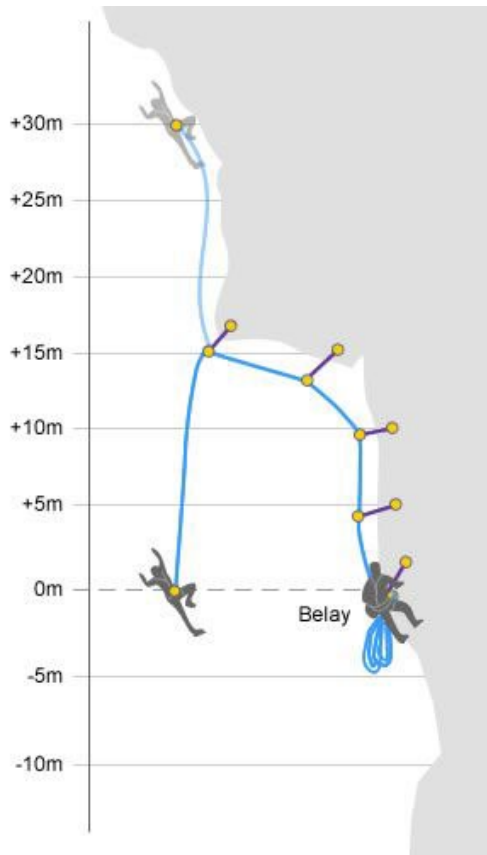
$$s_4 = 6,7449 \text{ kJ/kg/K}$$

$$T_{\text{sat}} = 233,8 \text{ °C}$$

$$P_s = 1,231 \text{ MPa}$$

$$h_4 = 2897,0 \text{ kJ/kg}$$





$350^{\circ}\text{C} @ 1,231 \text{ MPa}$



$$h_5 = 3153,5 \text{ kJ/kg}$$

$$s_5 = 7,2012 \text{ kJ/kg/K}$$

$S_5 = S_6 @ 75\text{kPa}$



$$s_{\text{liq}} = 1,2132 \text{ kJ/kg/K}$$

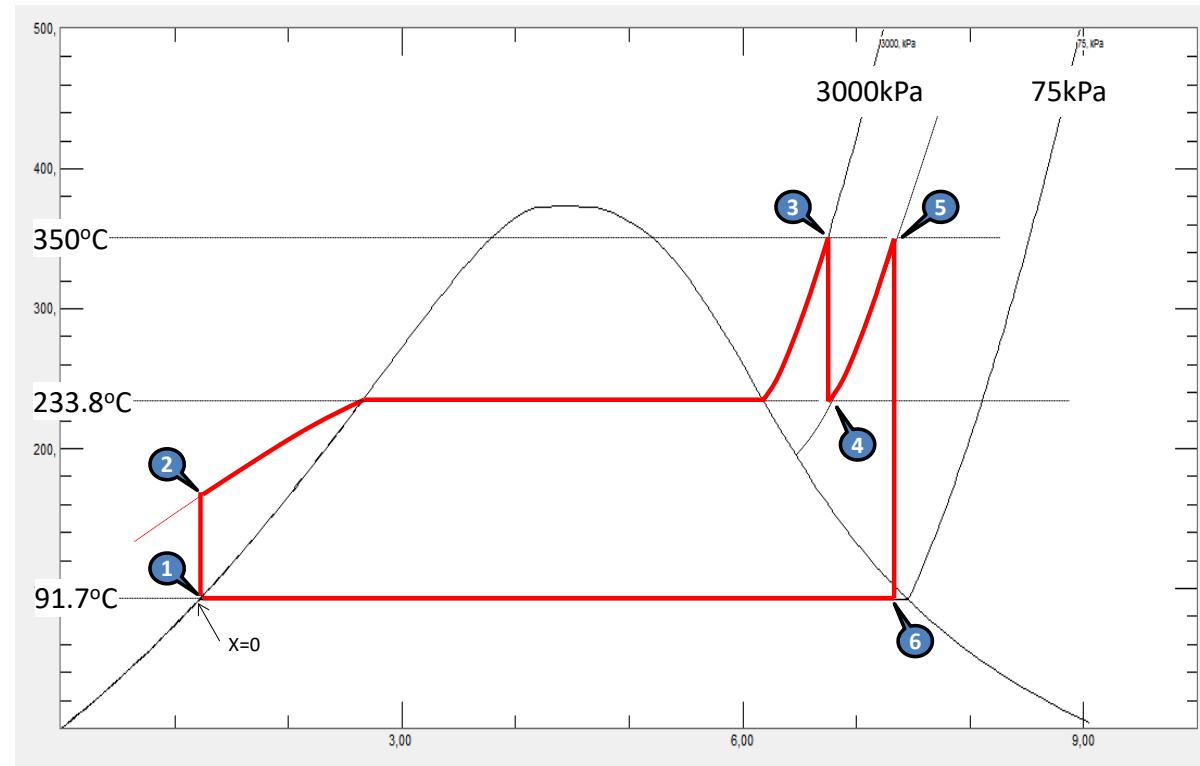
$$s_{\text{vap}} = 7,4557 \text{ kJ/kg/K}$$

$$x = 0,959$$

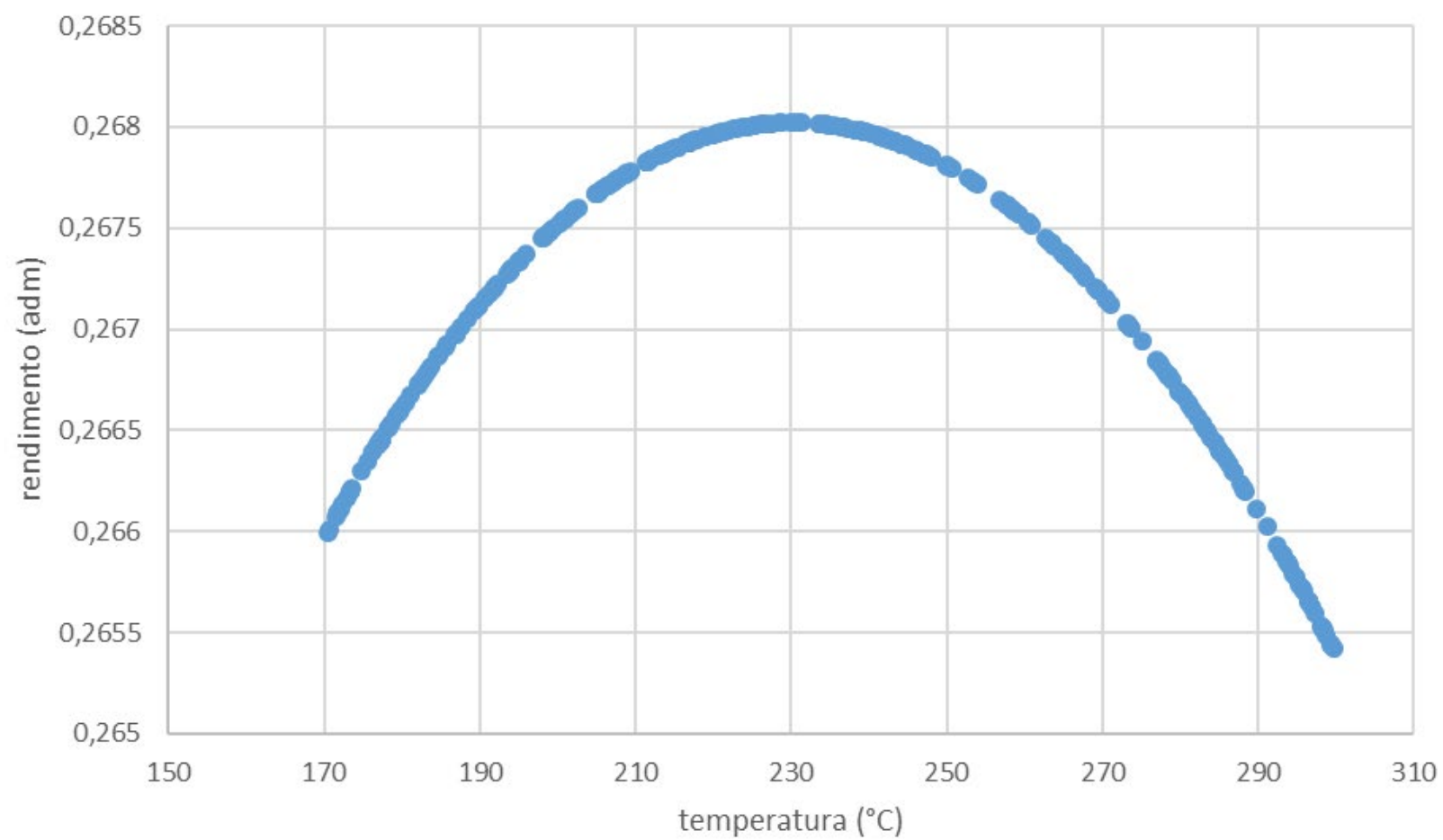
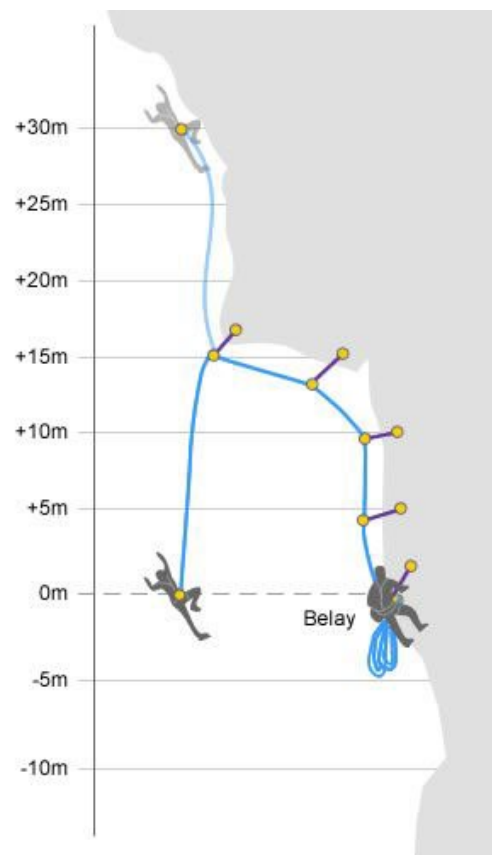
$$h_{\text{liq}} = 384,44 \text{ kJ/kg}$$

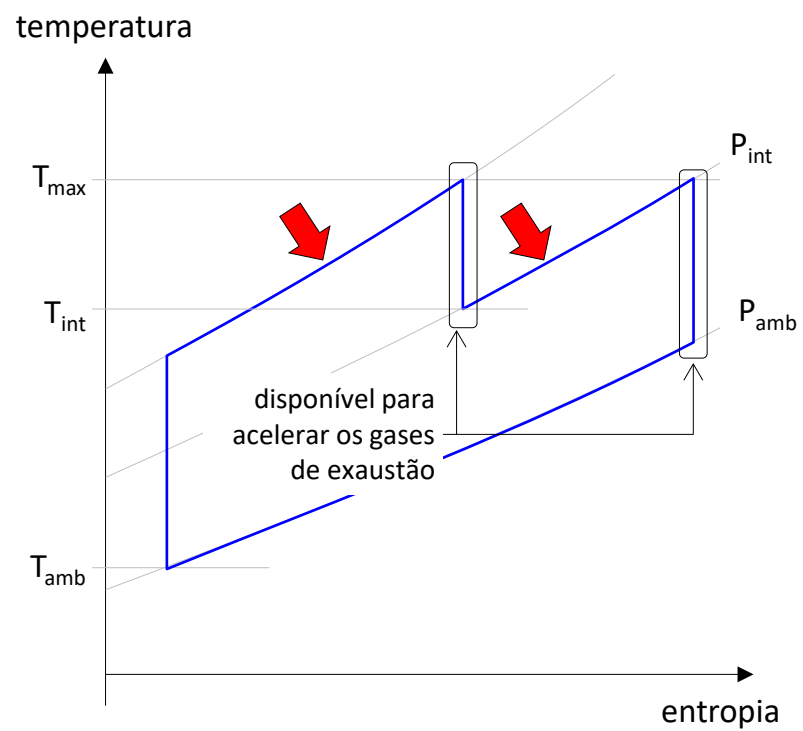
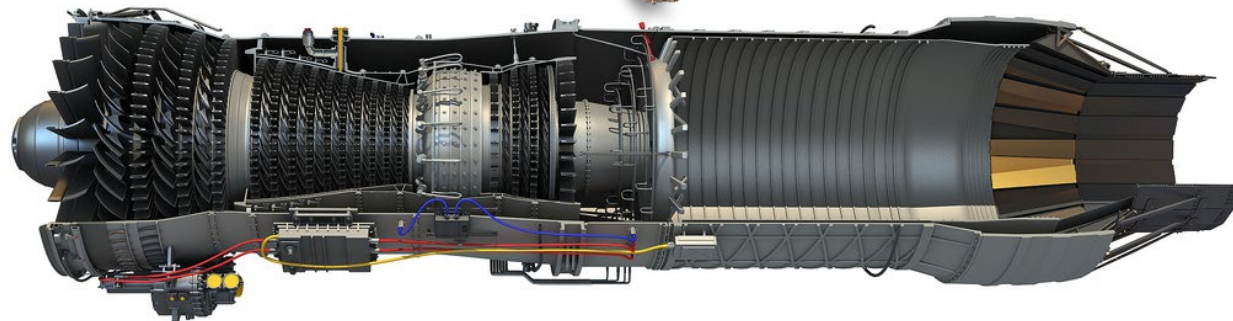
$$h_{\text{vap}} = 2662,4$$

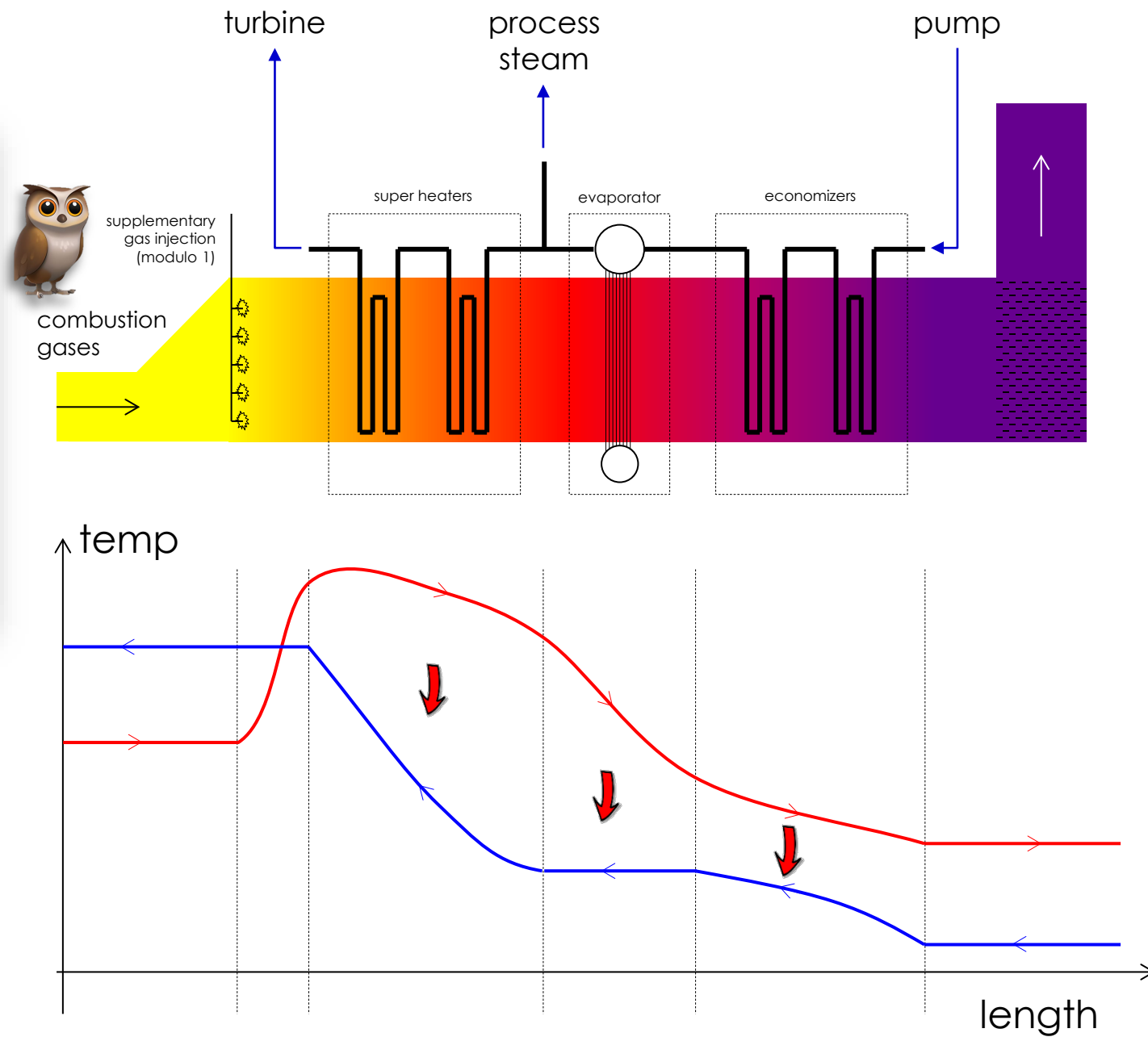
$$h_6 = 2569,0 \text{ kJ/kg}$$





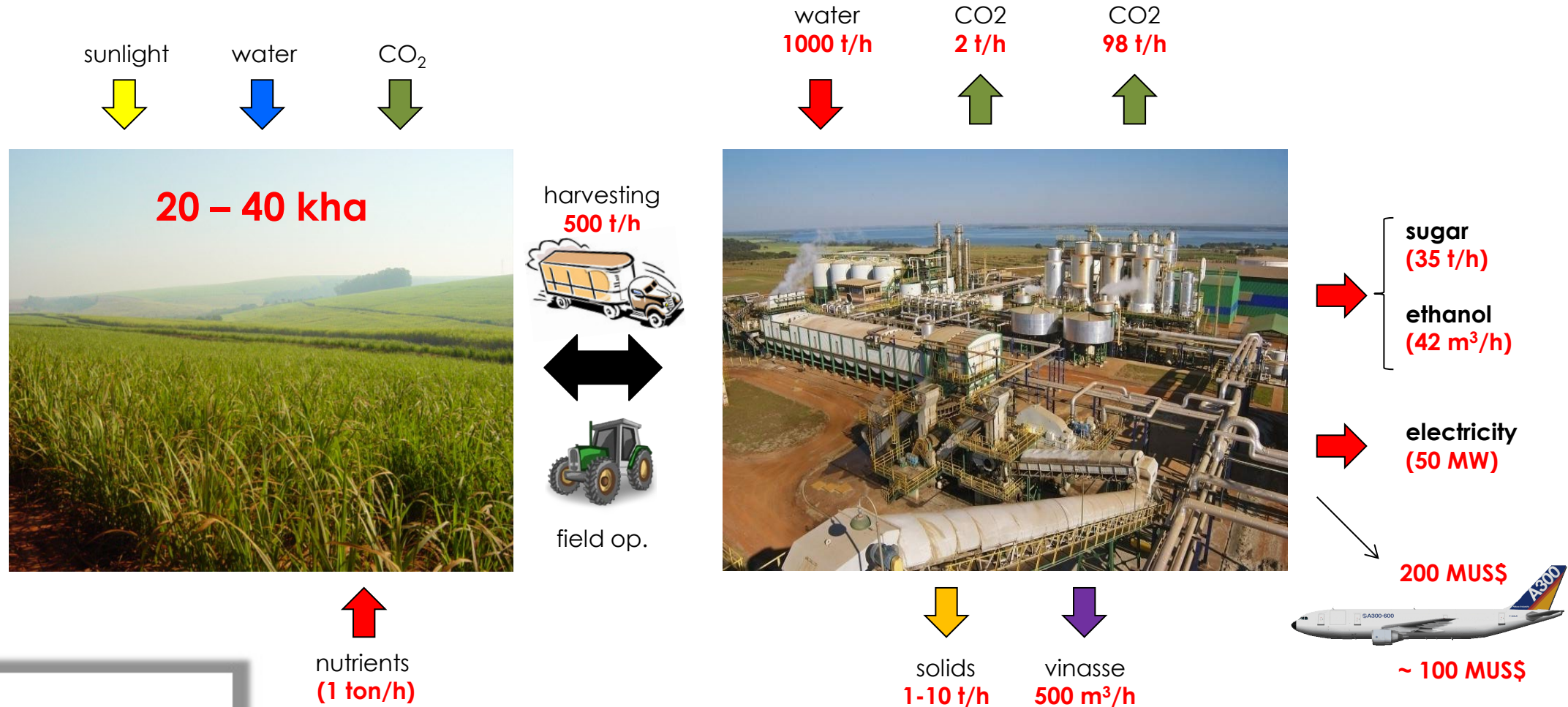






# APLICAÇÕES COM DEMANDA SIMULTÂNEA DE TRABALHO MECÂNICO E CALOR DE PROCESSO

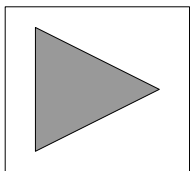
# USINA DE CANA DE AÇÚCAR CONVENCIONAL – AÇÚCAR, ETANOL E ELETRICIDADE



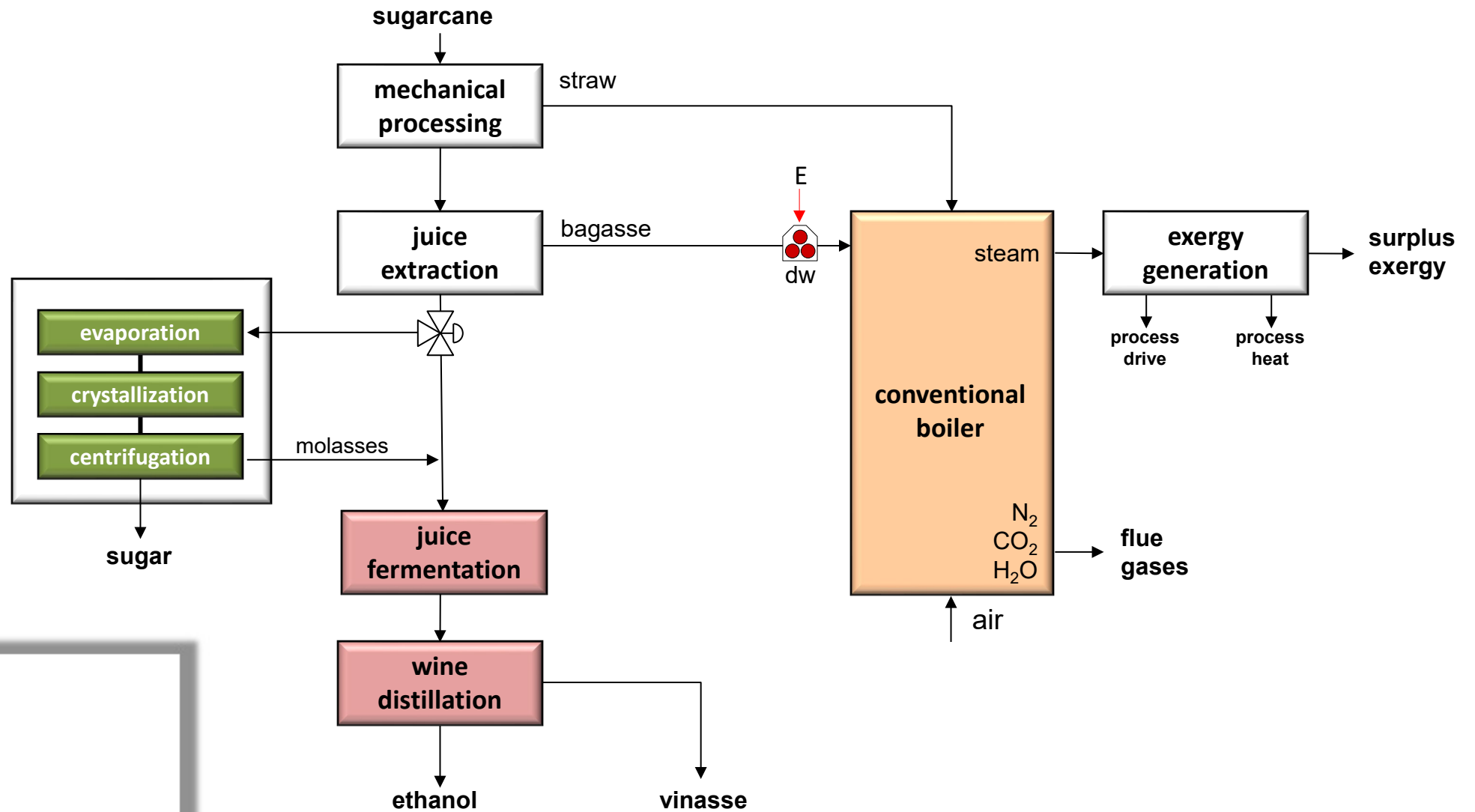
Attention to  
Filler Words

TRL 9 → “Turn Key” contracts

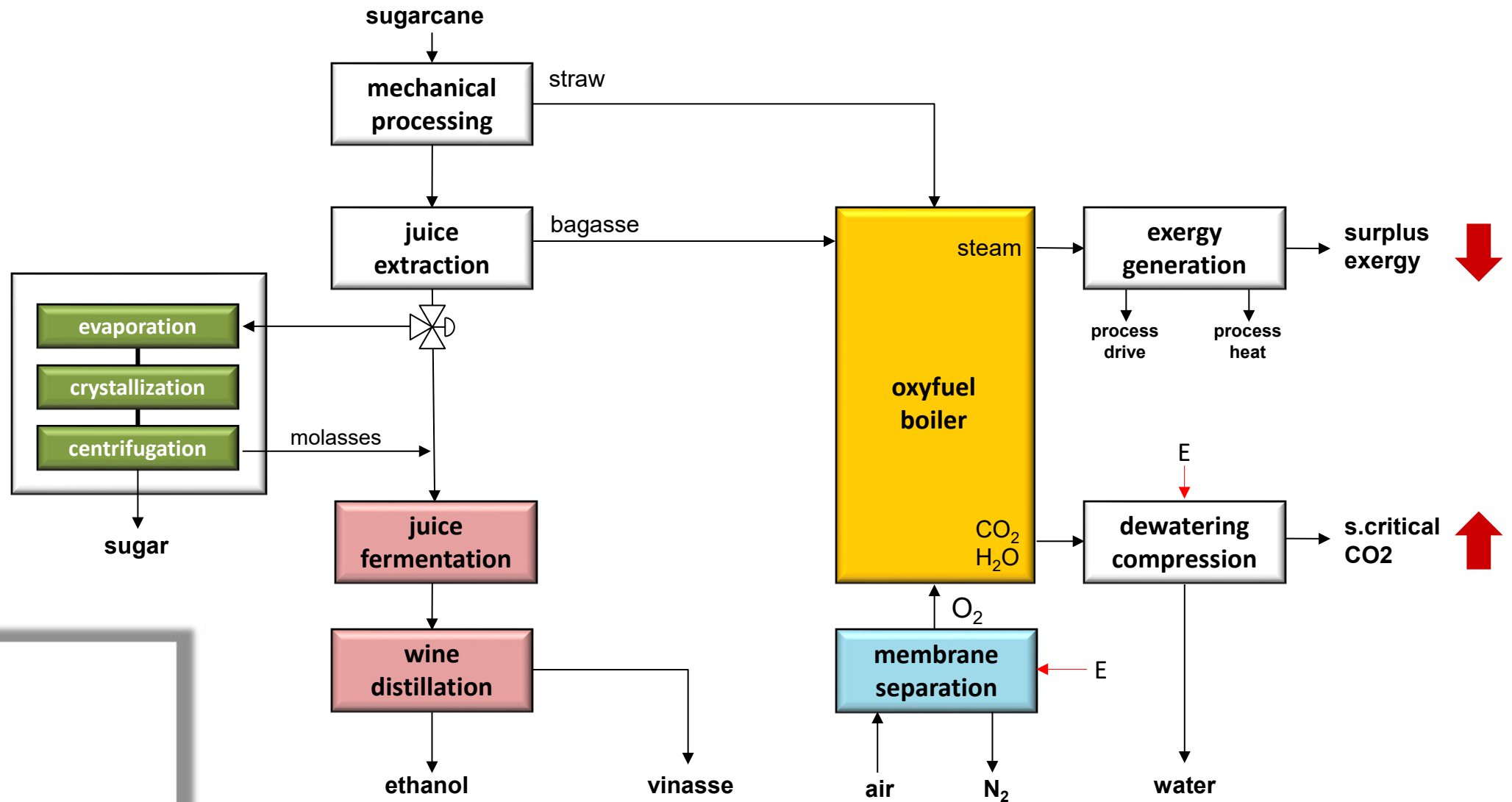
# USINA DE CANA DE AÇÚCAR CONVENCIONAL – AÇÚCAR, ETANOL E ELETRICIDADE



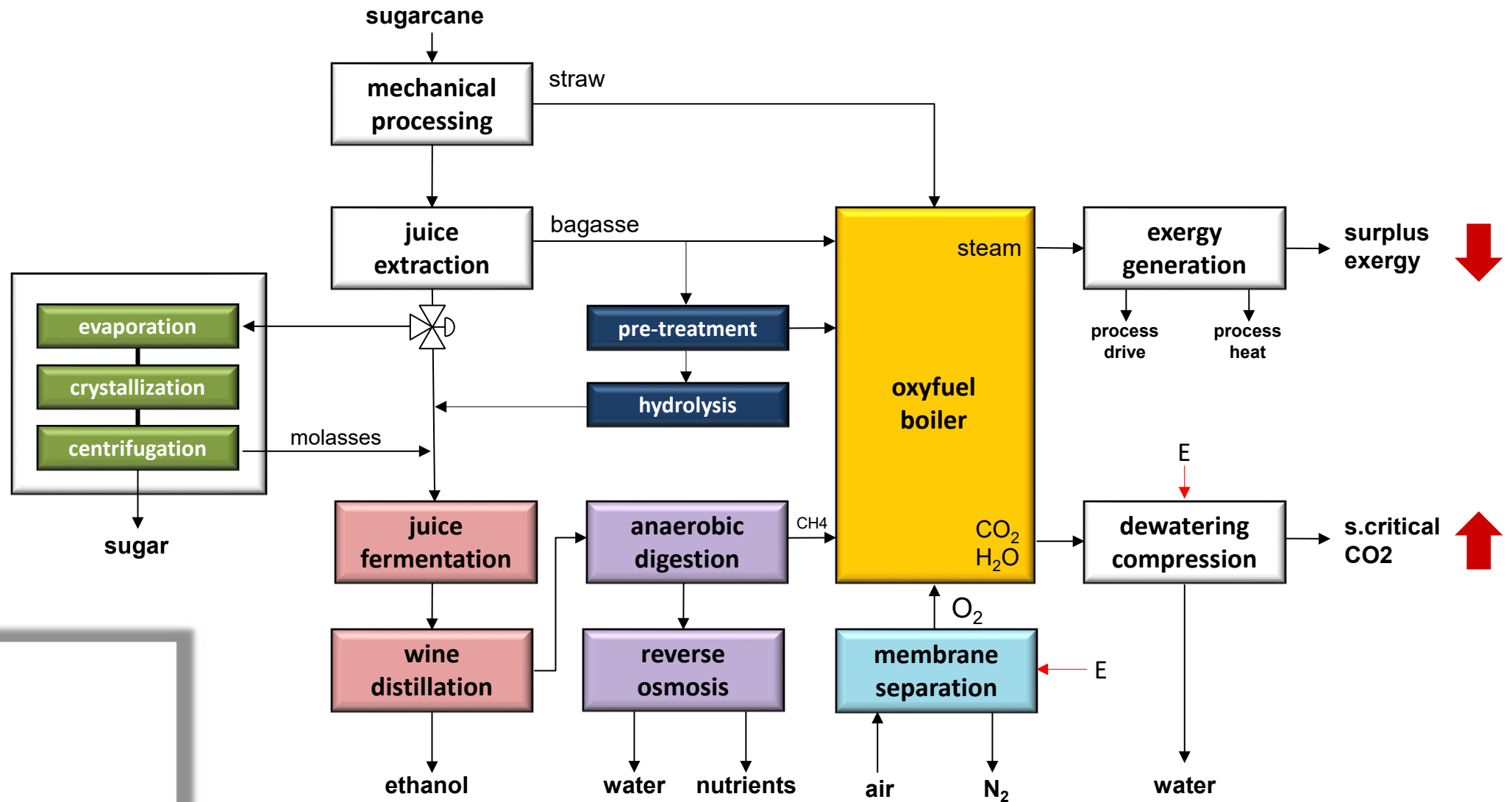
# USINA DE CANA DE AÇÚCAR CONVENCIONAL – AÇÚCAR, ETANOL E ELETRICIDADE

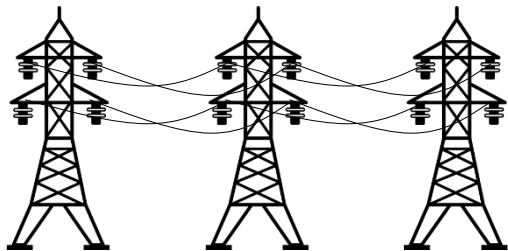


# USINA DE CANA DE AÇÚCAR AVANÇADA – AÇÚCAR, ETANOL, ELETRICIDADE, CO2 SUPERCRÍTICO, ETC.



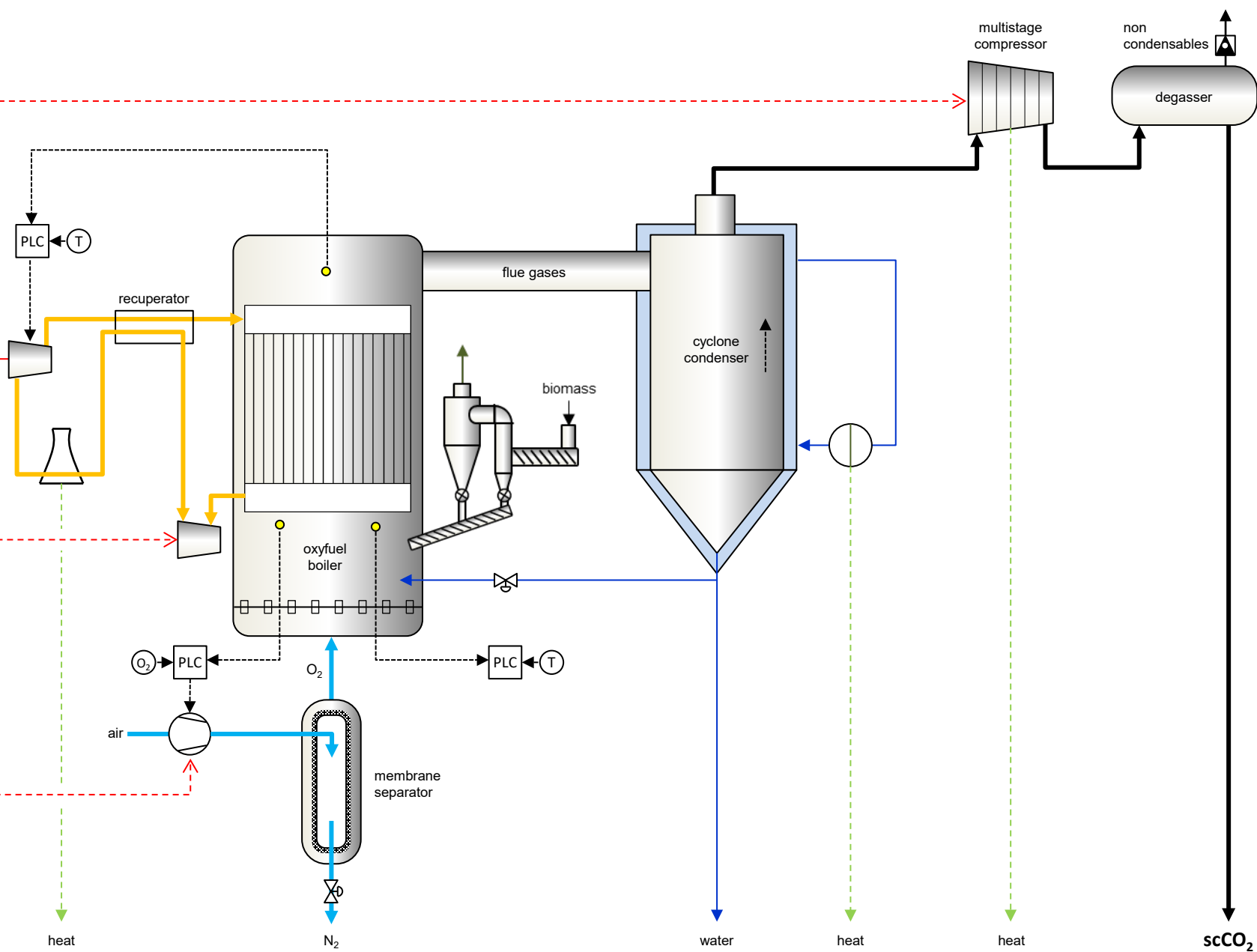
# USINA DE CANA DE AÇÚCAR AVANÇADA – AÇÚCAR, ETANOL, ELETRICIDADE, CO2 SUPERCRÍTICO, ETC.

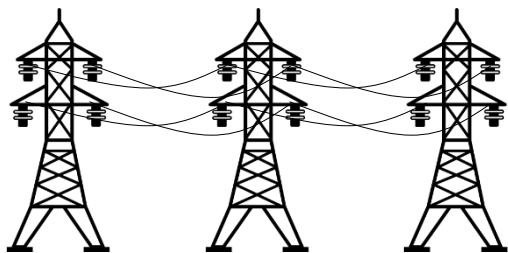




surplus

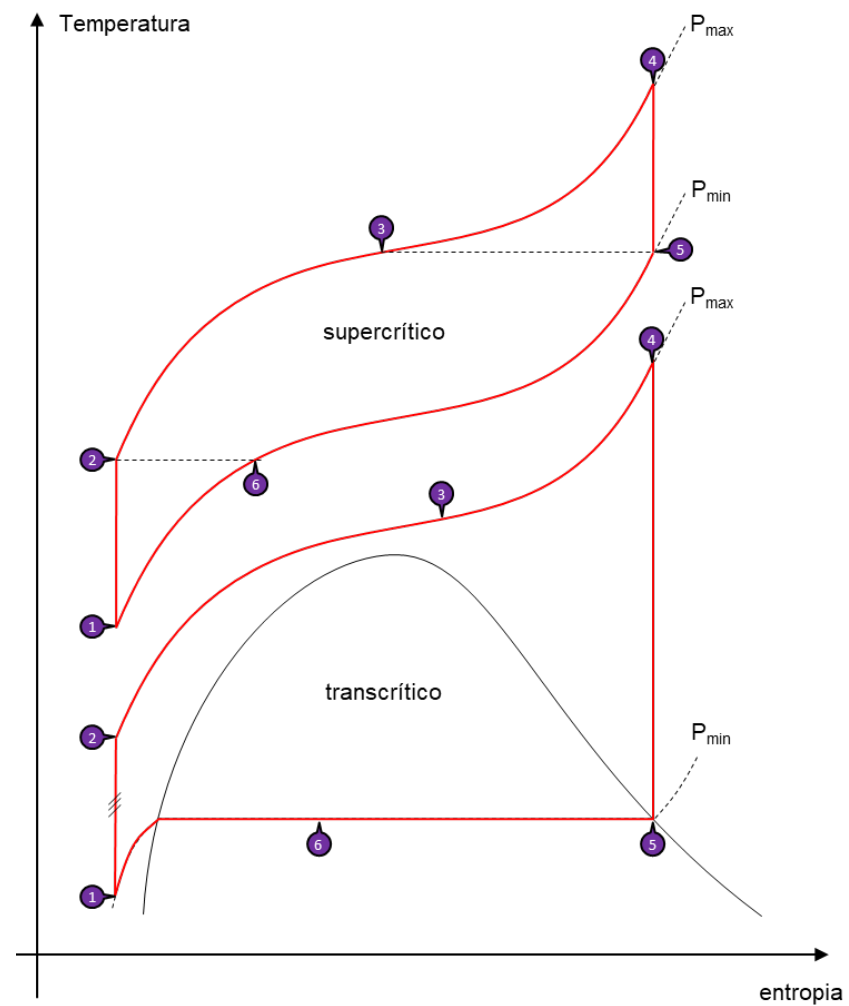
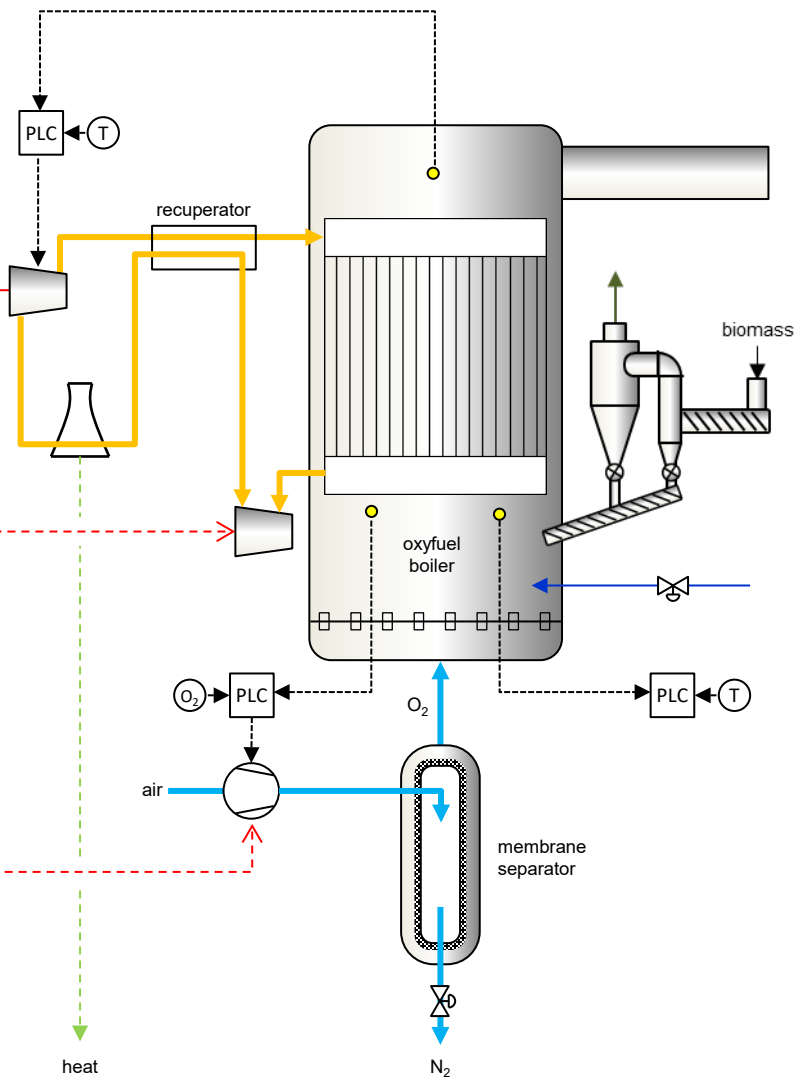
process

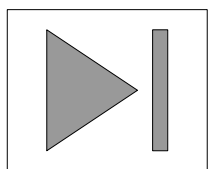
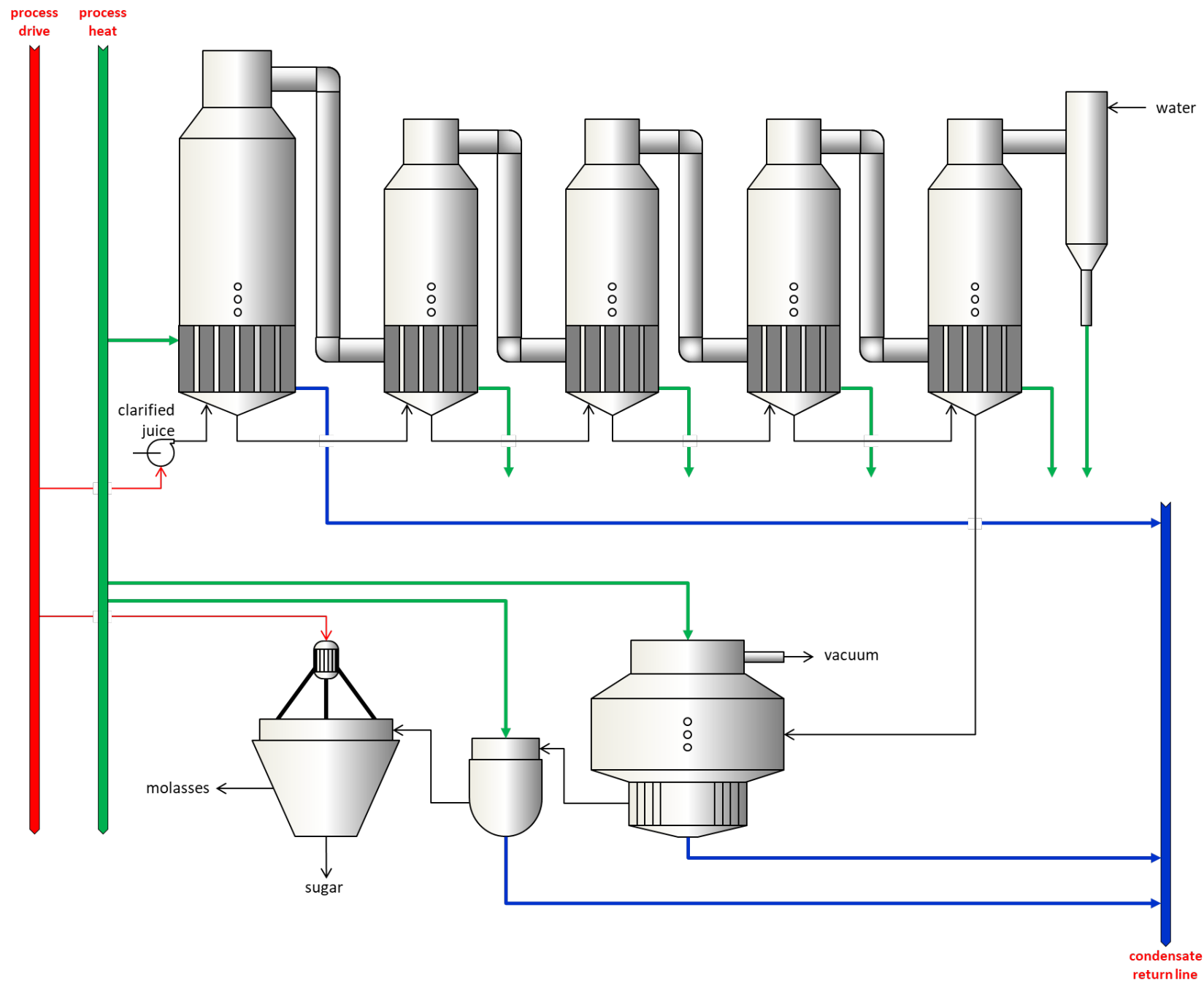
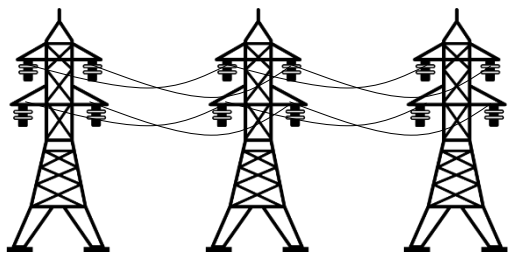




surplus

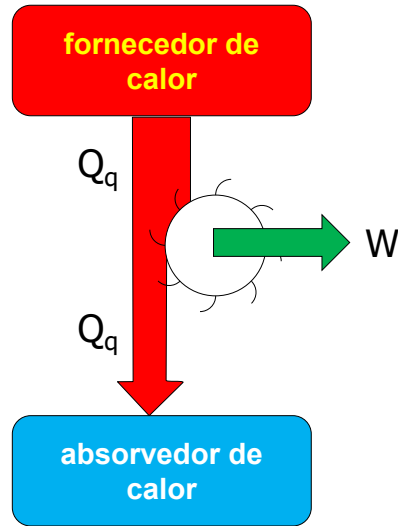
process







# Aproveitamento do calor rejeitado (2ª Lei da Termodinâmica)



1º Lei:  $Q_q = Q_f + W$

2º Lei:  $W/Q_q < 100\%$

$$\eta_{\text{cog}} \hat{=} \frac{W_{\text{liq}} + Q_{\text{proc}}}{Q_q} \leq 1$$

$$\eta_{\text{cog}} = \left| \frac{m_{\text{ciclo}} \cdot [(h_3 - h_4) - (h_2 - h_1)] + m_{\text{proc}} \cdot (h_4 - h_1)}{m_{\text{ciclo}} \cdot (h_3 - h_2)} \right|$$

↓  $m_{\text{ciclo}} = m_{\text{proc}}$

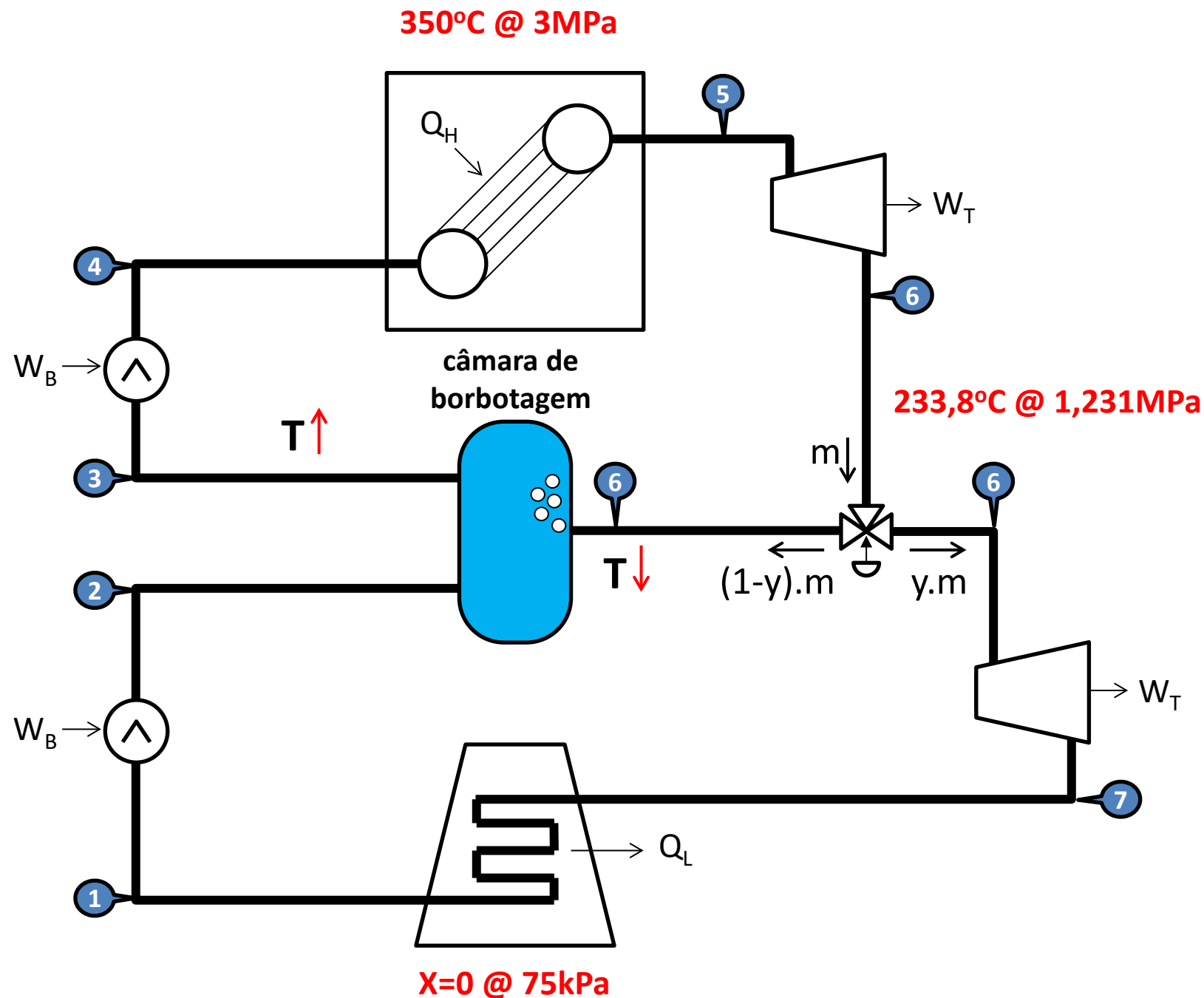
$$\eta_{\text{cog}} = \left| \frac{[(h_3 - h_4) - (h_2 - h_1)] + (h_4 - h_1)}{(h_3 - h_2)} \right|$$

$$\eta_{\text{cog}} = 1$$

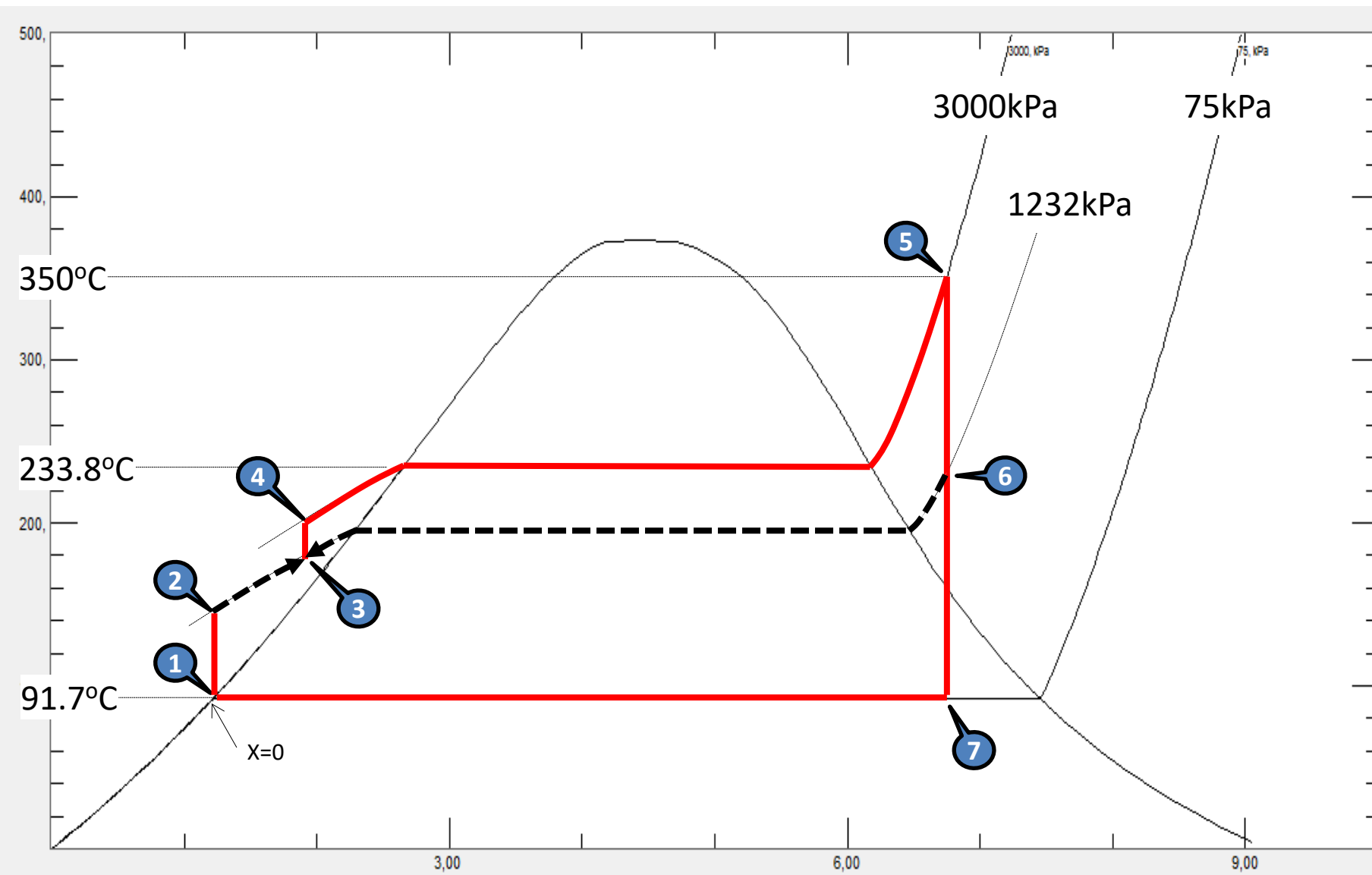
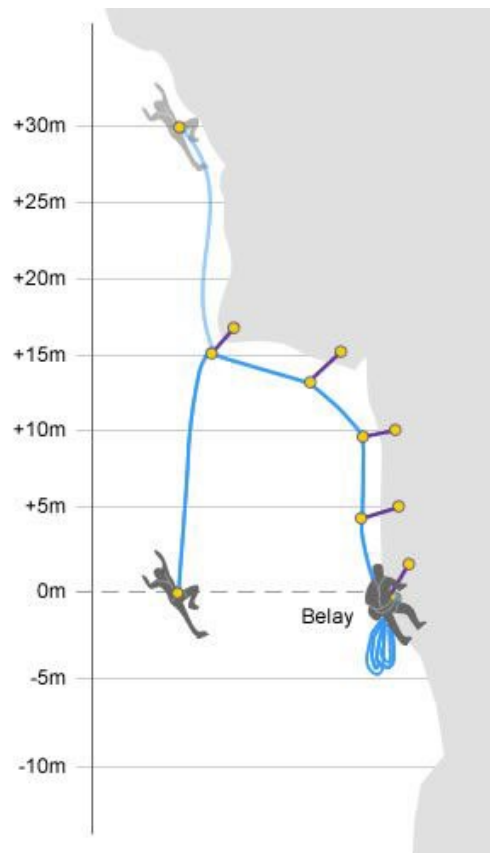
# **Ciclo de Rankine com aquecimento regenerativo**

$$\eta = \frac{w_{12} + w_{34} + w_{56} + w_{67}}{q_{45}}$$

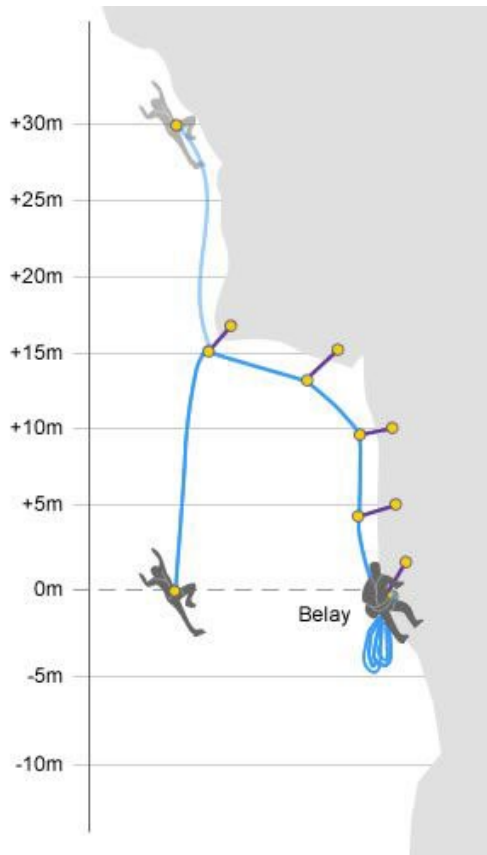
Attention to  
Filler Words



temperatura °C



entropia kJ/kg/K



$$x = 0 @ 75\text{kPa}$$



$$h_1 = 384,44 \text{ kJ/kg/K}$$

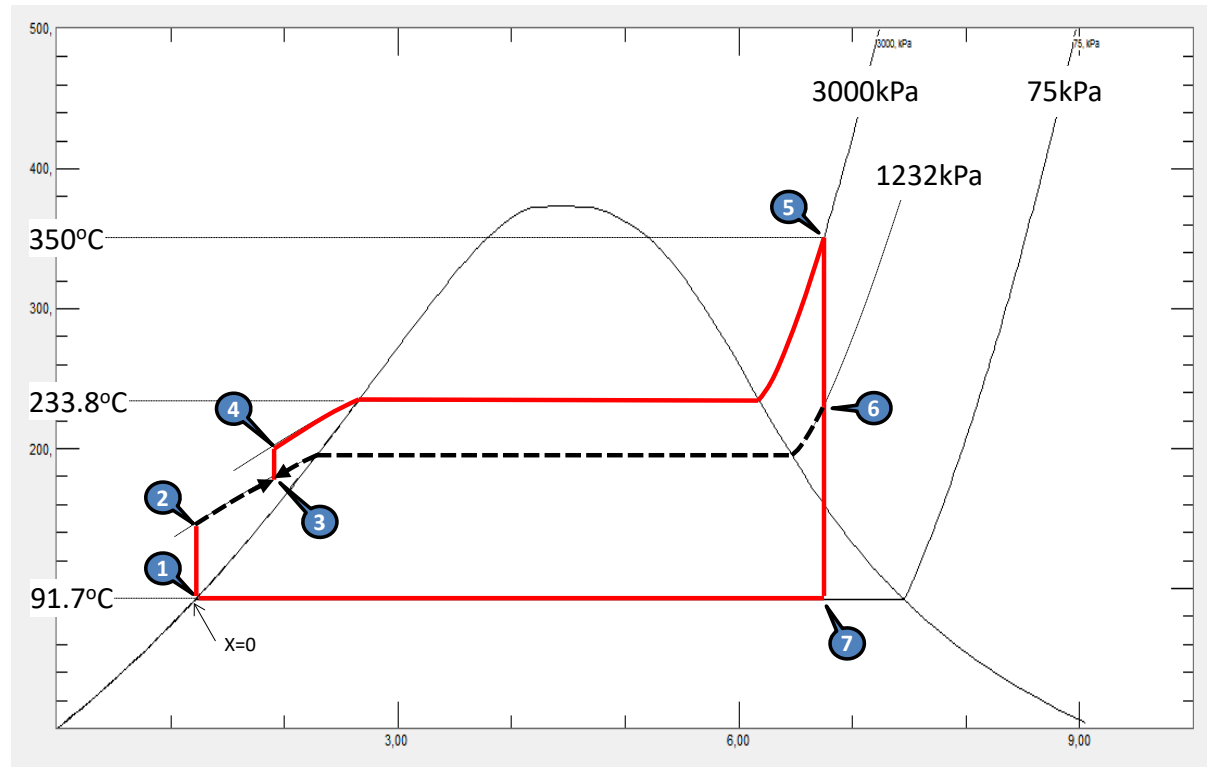
$$s_1 = 1,2132 \text{ kJ/kg/K}$$

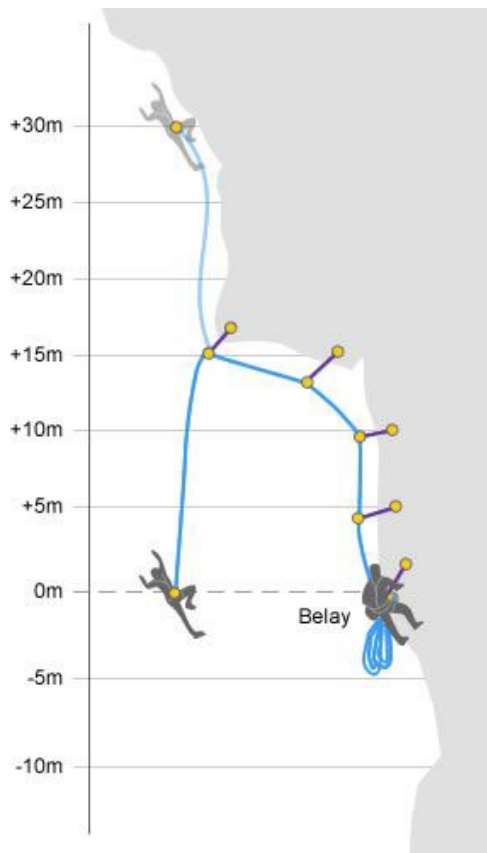
$$S_1 = S_2 @ 1,231\text{MPa}$$



$$h_2 = 385,65 \text{ kJ/kg/K}$$

$$T_2 = 91,834 \text{ }^{\circ}\text{C}$$





equação de mistura



$$h_3 = \dots$$

$$h_4 = \dots$$

$$s_3 = \dots$$

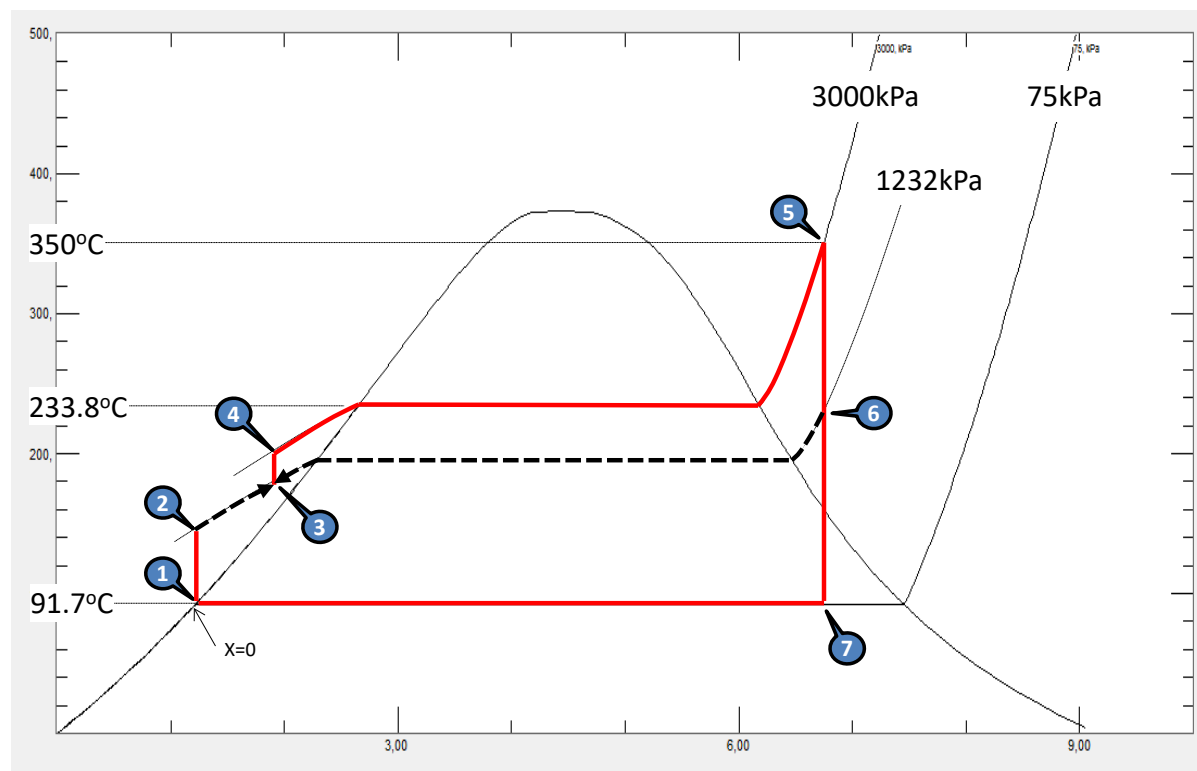
$$s_4 = \dots$$

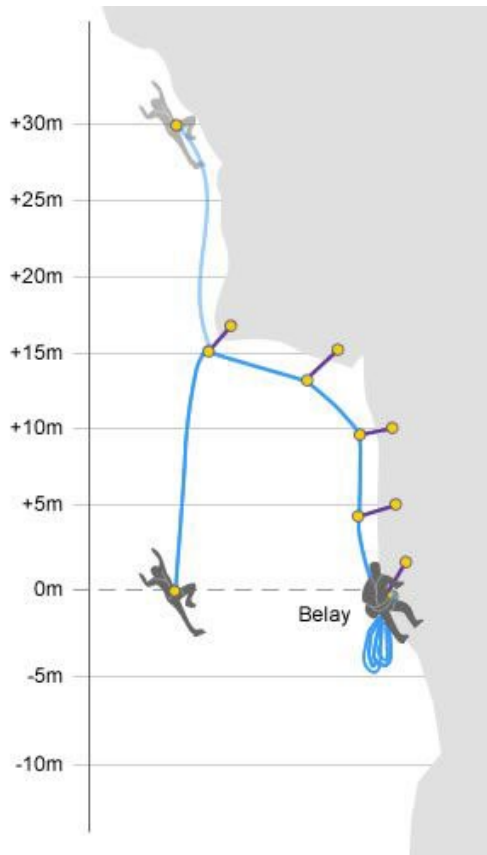
350°C @ 3 MPa



$$h_5 = 3116,1 \text{ kJ/kg}$$

$$s_5 = 6,7449 \text{ kJ/kg/K}$$





$$S_5 = S_6 @ 1,231 \text{ MPa}$$



$$h_6 = 2896,9 \text{ kJ/kg}$$

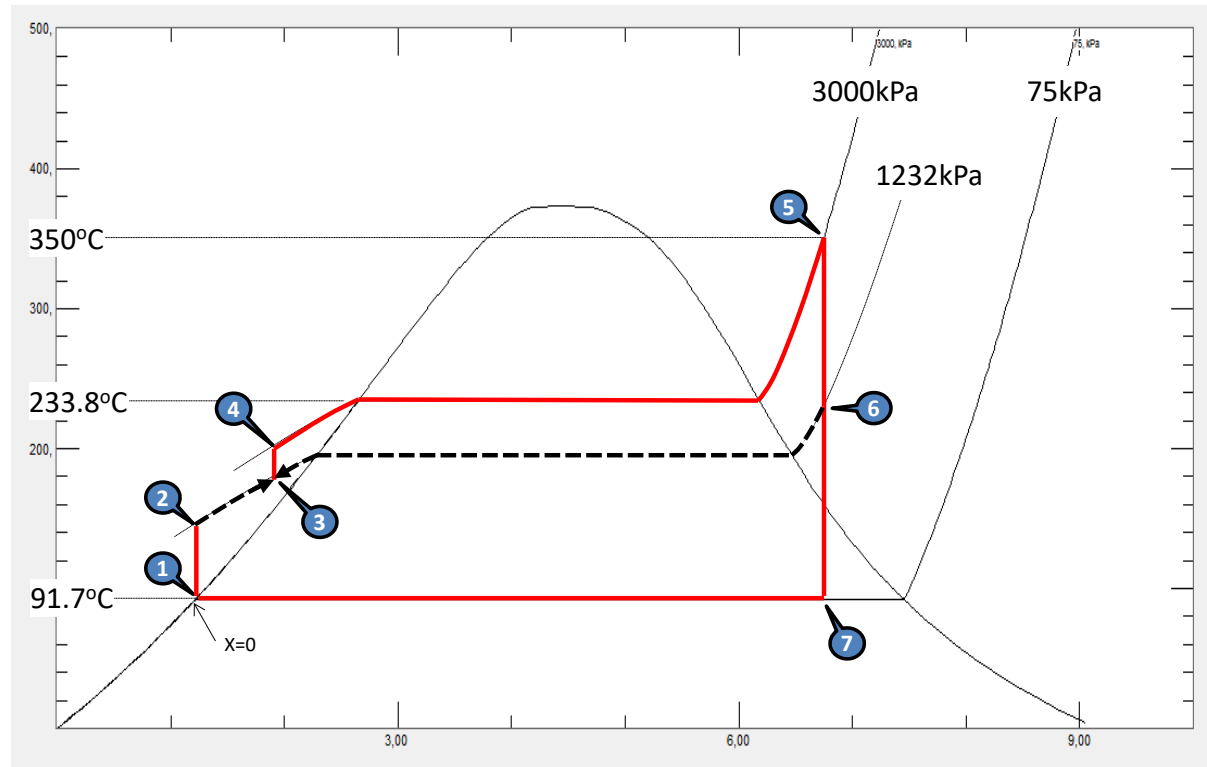
$$s_6 = 6,7449 \text{ kJ/kg/K}$$

$$S_6 = S_7 @ 75 \text{ kPa}$$



$$h_7 = 2403,0 \text{ kJ/kg}$$

$$x_7 = 0,88614 \text{ kg/kg}$$

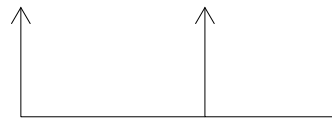


# Determinação do estado da mistura vapor/líquido

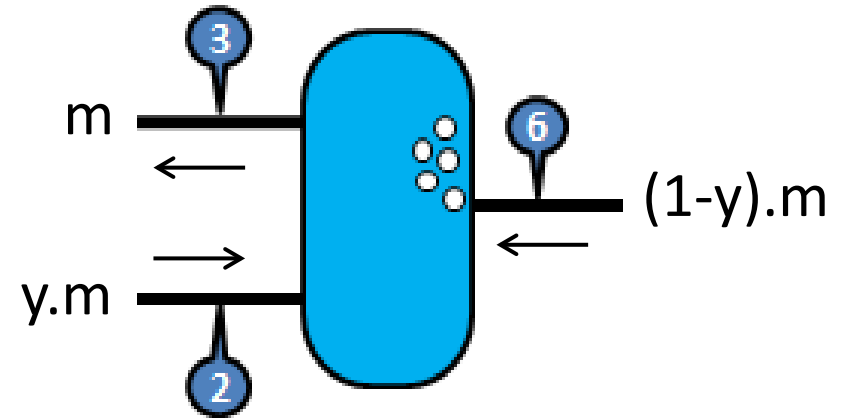
$$h_3 = (1-y) \cdot h_6 + y \cdot h_2$$

$$h_3 \leq h_{\text{sat,liq}} \mid_{1,23\text{MPa}} = 803,64 \text{ kJ/kg}$$

$$s_3 = h[ P_3, h_3(y) ]$$



Parâmetros arbitrados no projeto (e.g.  $y = 0,98$ ,  $P_3 = 12,31\text{bar}$ )



$$h_3 = (1-0.98) \cdot 2896,9 + 0,98 \cdot 385,65 = 435.87 \text{ kJ/kg}$$

$$s_3 = h(P_3, h_3) = 1,3486 \text{ kJ/kg/K} \quad s_3 \stackrel{?}{=} (1-y) \cdot s_6 + y \cdot s_2$$

$$s_3 \stackrel{?}{>} (1-0.98) \cdot 6,7449 + 0,98 \cdot 1,2132 = 1,324 \text{ kJ/kg/K}$$

O processo de mistura  
gera entropia



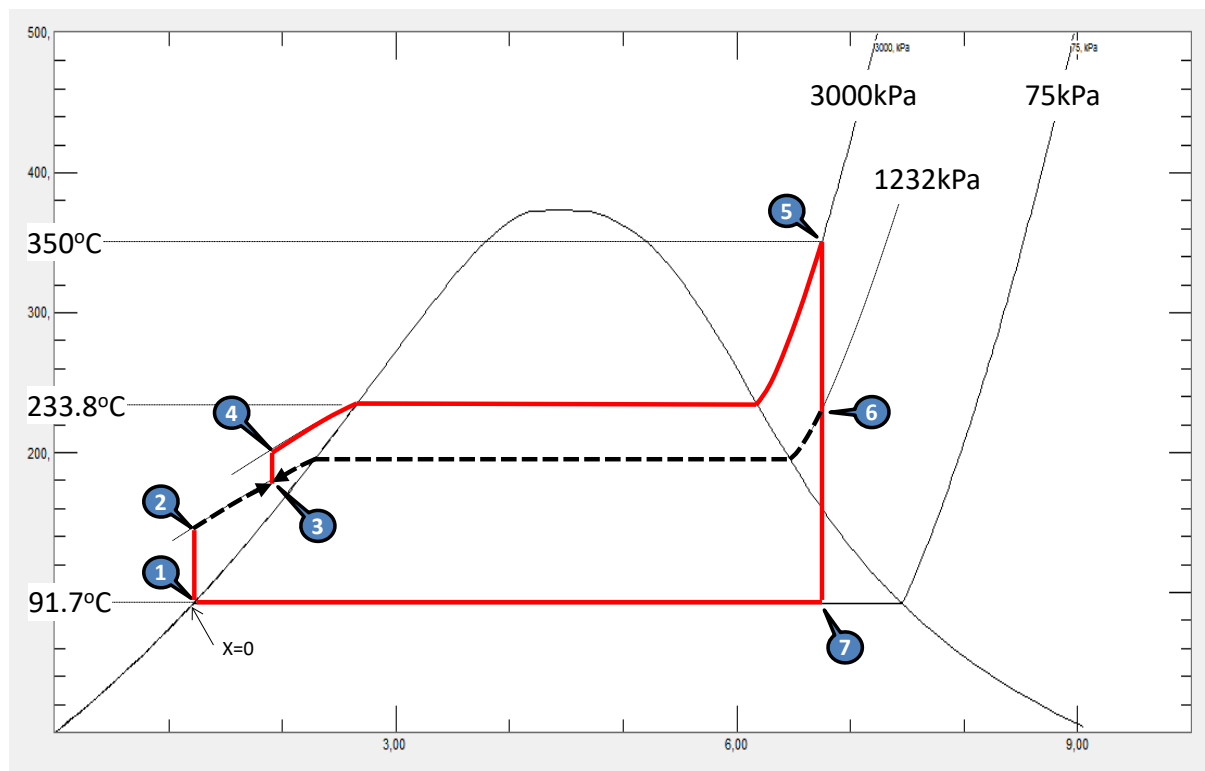
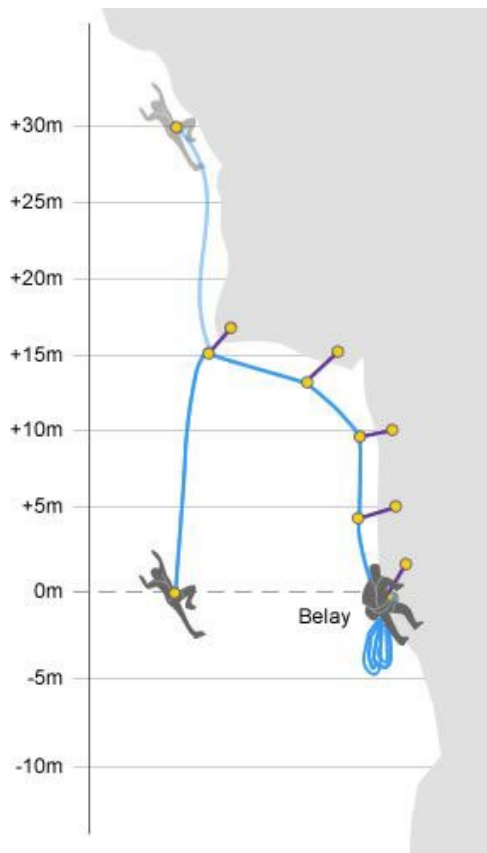
equação de mistura



$$P_4 = 3000 \text{ kPa}$$

$$h_4 = 437,72 \text{ kJ/kg/K}$$

$$s_4 = 1,3486 \text{ kJ/kg/K}$$



$$\eta = \frac{\sum W_T - \sum W_B}{\sum Q_C}$$

$$\eta = \frac{[m \cdot (h_5 - h_6) + ym \cdot (h_6 - h_7)] - [ym \cdot (h_2 - h_1) + m \cdot (h_4 - h_3)]}{m \cdot (h_5 - h_4)}$$

$$\eta = \frac{[\cancel{m} \cdot (h_5 - h_6) + y\cancel{m} \cdot (h_6 - h_7)] - [y\cancel{m} \cdot (h_2 - h_1) + \cancel{m} \cdot (h_4 - h_3)]}{\cancel{m} \cdot (h_5 - h_4)}$$

$$\eta = \frac{[(h_5 - h_6) + y \cdot (h_6 - h_7)] - [y \cdot (h_2 - h_1) + (h_4 - h_3)]}{(h_5 - h_4)}$$

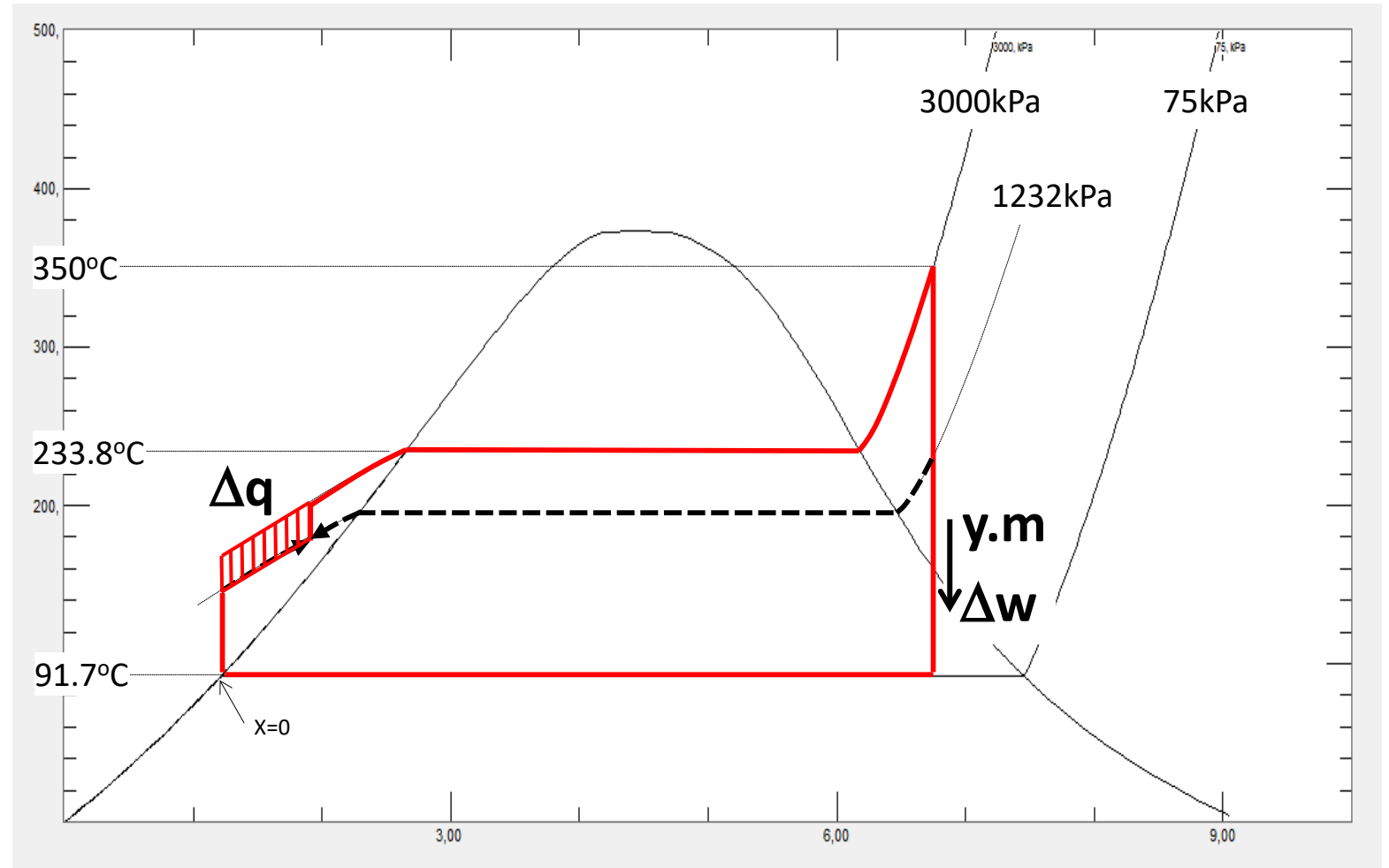
$$\eta_{\text{Rank}} = 0,263$$

$$\eta_{\text{reaq}} = 0,268$$

$$\eta_{\text{regen}} = 0,261$$

Devem ser  
comparadas as  
configs otimizadas

$$\eta = \frac{\downarrow\downarrow\downarrow w_t - w_b}{\downarrow q_c}$$



# Curso de Termodinâmica

## **CICLOS A VAPOR** **parte 1/2**



**aula 12/20**